High-resolution CO and radio imaging of $z \sim 2$ ULIRGs: extended CO structures and implications for the universal star formation law


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ABSTRACT
We present high spatial resolution (0.4 arcsec, $\approx 3.5$ kpc) Plateau de Bure Interferometer interferometric data on three ultraluminous infrared galaxies (ULIRGs) at $z \sim 2$: two submillimetre galaxies (SMGs) and one submillimetre faint star-forming radio galaxy. The three galaxies have been robustly detected in CO rotational transitions, either $^{12}$CO ($J = 4 \rightarrow 3$) or $^{12}$CO ($J = 3 \rightarrow 2$), allowing their sizes and gas masses to be accurately constrained. These are the highest spatial resolution observations observed to date (by a factor of $\approx 2$) for intermediate-excitation CO emission in $z \sim 2$ ULIRGs. The galaxies appear extended over several resolution elements, having a mean radius of 3.7 kpc. High-resolution (0.3 arcsec) combined Multi-Element Radio-Linked Interferometer Network-Very Large Array observations of their radio continua allow an analysis of the star formation behaviour of these galaxies, on comparable spatial scales to those of the CO observations. This ‘matched beam’ approach sheds light on the spatial distribution of both molecular gas and star formation, and we can therefore calculate accurate star formation rates and gas surface densities: this allows us to place the three systems in the context of a Kennicutt–Schmidt (KS)-style star formation law. We find a difference in size between the CO and radio emission regions, and as such we suggest that using the spatial extent of the CO emission region to estimate the surface density of star formation may lead to error. This size difference also causes the star formation efficiencies within systems to vary by up to a factor of 5. We also find, with our new accurate sizes, that SMGs lie significantly above the KS relation, indicating that stars are formed more efficiently in these extreme systems than in other high-$z$ star-forming galaxies.

Key words: galaxies: evolution – galaxies: formation – galaxies: ISM – cosmology: observations.

1 INTRODUCTION
Recent evidence has suggested that the star formation activity of the Universe peaks at redshifts between 1 and 3, and as such an understanding of the systems involved in forming stars at these cosmological redshifts is of great importance. Of particular interest are
the luminous submillimetre galaxies (SMGs; Smail et al. 2002), which peak strongly at $z \sim 2$ (Chapman et al. 2005). First detected with the Submillimeter Common-User Bolometer Array (SCUBA; Holland et al. 1999), these sub-mm-selected ($S_{850, \mu m} \gtrsim 3$ mJy) systems have prodigious star formation rates (SFR) which are an order of magnitude greater than optically selected galaxies at comparable redshifts ($\gtrsim 1000$ M$_{\odot}$ yr$^{-1}$), large reservoirs of molecular gas ($\sim 10^{10}$ M$_{\odot}$; Greve et al. 2005) and are thought to contribute a substantial fraction of the total cosmic SFR density at their peak epoch ($\sim 50$ per cent at $z \sim 2$; Blain et al. 1999, 2002). Being sub-mm selected, the bolometric emission from these systems is dominated by cold dust ($T_d \lesssim 30$ K), and they are relatively faint at 24 $\mu$m and in the X-ray, indicating that the contribution from an active galactic nucleus (AGN) component is generally negligible.

Observations of CO structures in SMGs have generally suggested relatively small spatial extents (Tacconi et al. 2008), typically having half-light radii on the order of 2 kpc. This, combined with the massive reservoir of gas in the interstellar medium (ISM), leads to a very high density (up to two orders of magnitude denser than their optically selected counterparts; Nesvadba et al. 2007) which triggers the intense starbursting behaviour that is characteristic of the SMG population. Many authors have concluded that the SMGs are therefore ‘scaled-up’ versions of ultraluminous infrared galaxies (ULIRGs; galaxies with $L_{IR} > 10^{12}$ L$_{\odot}$), in the local Universe, being a population of compact star-forming galaxies driven by major mergers (Sanders & Mirabel 1996) with CO sizes comparable to the radii of the entire galaxy (Tacconi et al. 1999; Iono et al. 2007). In this model, the star formation is concentrated entirely in the dense circumnuclear region. Recent work has drawn upon evidence from features in the mid-IR (e.g. polycyclic aromatic hydrocarbon (PAH) emission in the study of Menéndez-Delmestre et al. (2009) and near-IR colours in the work of Hainline et al. (2009)], using measures of the extinction to infer that the star-forming region in SMGs is extended on scales of $>2$ kpc, proportionally far larger than anything seen in local ULIRGs. It remains to be seen therefore whether conventional star formation prescriptions applicable to galaxies in the low-redshift universe can account for the extreme star-forming behaviour seen in SMGs.

In this paper, we report the Institut de Radioastronomie Millimétrique (IRAM) Plateau de Bure Interferometer (PdBI) observations of three high-redshift star-forming sources. Combined Multi-Element Radio-Linked Interferometer Network (MERLIN) + Very Large Array (VLA) radio continuum observations are used to analyse the spatially resolved star formation behaviour (e.g. Chapman et al. 2004; Muxlow et al. 2005; Biggs & Ivison 2008; Casey et al. 2009a), in combination with the spatially resolved information on the molecular gas content provided by the PdBI, to attempt to analyse the connection between the gas content and star formation behaviour in these extreme high-redshift systems. The high-resolution analysis of both the PdBI and MERLIN observations allows the sizes of the CO and star-forming regions to be ascertainment accurately and independently, allowing for accurate measurements of both the SFR surface density and the molecular gas surface density. As such, we can place our sources in the context of the Kennicutt–Schmidt (KS) law, which has been proposed as a possible ‘universal star formation law’ (Bouché et al. 2007).

In Section 2 we outline the observations behind this work, and in Section 2.3 we outline the techniques used to analyse our data. In Section 3 we individually discuss our galaxies, in terms of their CO properties, star formation behaviour and kinematical parameters. Section 4 contains a further discussion of merger versus disc scenarios and star formation efficiencies for our galaxies, and attempts to place them in the context of a KS star formation law, and we conclude in Section 5.

Throughout this work, we assume a concordance $\Lambda$ cold dark matter ($\Lambda$CDM) cosmology with $h = 0.71$, $\Omega_\Lambda = 0.72$ and $\Omega_M = 0.28$.

2 OBSERVATIONS AND ANALYSIS

We aim to compare matched beam ($\sim 0.4$ arcsec) observations of mid-excitation CO lines and radio continua in a selection of $z \sim 2$ ULIRGs, two in the Hubble Deep Field (HDF)-North and one in the Lockman hole, whose optical counterparts have been identified as HDF 132 ($z = 1.999$), HDF 254 ($z = 1.996$) and Lockman 38 ($z = 1.523$), respectively. In this work, they are referred to as such hereafter. This project was undertaken with a long-term goal of including similarly high resolution of the resolved sub-mm continuum in order to fully characterize the nature of star formation, gas content and dust in these extreme systems. We have chosen three sources with good CO detections which have been well detected with MERLIN radio observations. In particular, the radio properties of the three sources were chosen to be representative of the SMG radio population as a whole (see Chapman et al. 2004), with $\sim 1/3$ being extended in the radio (HDF 254) and $\sim 2/3$ being radio compact (HDF 132 and Lockman 38), so the large CO structures discussed below do not result from a selection bias.

The three sources also span the complete range of $z \sim 2$ ULIRG spectral energy distribution (SED) types – Lockman 38 suggests a unusually cold SED, with a dust temperature $T_d \sim 20$ K. HDF 254 suggests a hot SED, with a $T_d$ of $65 \pm 14$ K (Casey et al. 2009c): it is strong in the radio, weak in the sub-mm and has significant 70 $\mu$m emission; it is, in fact, one of the few $z > 1$ ULIRGs (<5 percent) detected by Spitzer at 70 $\mu$m. HDF 132 is intermediate between these two sources, with an estimated $T_d$ of 40 K (Chapman et al. 2005).

2.1 PdBI CO observations

We observed CO rotation lines in the sub-mm faint star-forming radio galaxy (SFRG) RG J123711.34+621331.0 (= HDF 254), the sub-mm galaxy SMM J123618.33+621550.5 (= HDF 132) and the SMG SMM J105307+572431.4 (= Lockman 38) during 2009 February and March, using between four and six of the antennas (of a total of six). All sources were observed with the ‘long-baseline’ A configuration.

HDF 132 was observed in $^{12}$CO ($J = 4 \rightarrow 3$) on 2009 February 15 and 19, with on-source integration times of 8.9 and 2.9 h, respectively. Four of the six antennas were used. The observed frequency of the $^{12}$CO ($J = 4 \rightarrow 3$) line was 154.004 GHz, putting the CO-derived redshift at $z = 1.999 \pm 0.001$. HDF 254 was observed in $^{12}$CO ($J = 4 \rightarrow 3$) on 2009 February 16 with a total integration time of 6.2 h, using five antennas. $^{12}$CO ($J = 4 \rightarrow 3$) was observed at 154.122 GHz, setting the source at $z = 1.996 \pm 0.001$. Lockman 38 was observed with all six antennas on 2009 February 20 and March 12, with on-source integration times of 5.6 and 3.2 h, respectively. $^{12}$CO ($J = 3 \rightarrow 2$) was observed at 154.122 GHz, setting the source at $z = 1.523 \pm 0.002$. The synthesized beam size at 154 GHz is $\sim 0.4$ arcsec (Figures 1, 2 and 3; inset to middle panel), $\lesssim 3.4$ kpc at the redshifts of our sources.

The SMG SMM J123711.98+621325.7 (= HDF 255) was also within the field, being just 7 arcsec south-east of HDF 254. It was, however, undetected with our long-baseline configuration observations, which can be attributed to a combination of primary beam
Figure 1. HDF 132. Top left: stacked ACS image with overlaid CO emission contours (yellow) and NICMOS F160W contours (green). The yellow contours shown in the left-hand panel delineate the 97, 98, 99, 99.5 and 99.9th percentiles of the velocity-integrated CO data (the resultant levels in mJy beam$^{-1}$ are 0.43, 0.50, 0.74, 1.18 and 1.90, respectively). Bottom left: position–velocity diagram taken along the major axis of the galaxy (PA = 228°; defined by the position angle of the best-fitting ellipse to the CO map), with size and velocity scales shown in the inset. Centre: velocity-coded CO emission, with overlaid MERLIN 1.4 GHz radio contours (white; levels in $\mu$Jy beam$^{-1}$ are 10, 12, 34, 40 and 65). The inset velocity shift legend represents the centre of either the ‘red’ or the ‘blue’ bin, with respect to the centre of the ‘green’ central bin. The CO has been plotted starting at a significance level of 2$\sigma$ (in the integrated map); all points with detections < 2$\sigma$ have been left black. The radio beam has semimajor and semiminor axes of 0.204 × 0.193 arcsec$^2$, respectively. The outer contour of the inset ellipse (bottom left) corresponds to the FWHM of the CO beam, which is ~0.4 arcsec. Velocities are coded relative to the systemic velocity and are shown inset. Right: one-dimensional spectra, binned to 40 MHz, taken at the positions indicated. The spectra have been fitted with double-peaked Gaussian profiles.

The full width at half-maximum (FWHM) synthesized beam sizes for the maps are (semimajor axis versus semiminor axis in arcsec) 0.204 × 0.193, 0.205 × 0.192 and 0.5 × 0.5 for HDF 132, HDF 254 and Lockman 38, respectively. These beam sizes are all comparable in resolution to the long-baseline configuration beam size of the PdBI. The high spatial resolution of these observations allows for the star formation regions to be mapped in detail (rather than returning a single integrated value for the SFR), which is useful both for distinguishing point source AGN emission from diffuse star formation and for comparing the extent and shape of the star-forming region with the CO morphology (see Biggs & Ivison 2008). All three of our galaxies were well detected and fully resolved.

2.3 Analysis

Figs 1–3 show the CO observations and spectra, combined with optical images and MERLIN + VLA radio continuum observations (as detailed in the captions). Tables 1 and 2 contain the observational results and other derived parameters. All lines were successfully detected at a very high level of significance (>6$\sigma$).

The two HDF sources (132 and 254) have optical images comprised of $b$-, $v$-, $i$- and $z$-band images from the Advanced Camera for Surveys (ACS), stacked with equal weighting. In the case of HDF 132, Near-Infrared Camera and Multi-Object Spectrometer...
Figure 2. HDF 254. Top left: stacked ACS image with overlaid CO emission contours (yellow). The yellow contours shown in the left-hand panel delineate the 97, 98, 99, 99.5 and 99.9th percentiles of the velocity-integrated CO data (the resultant levels in mJy beam\(^{-1}\) are 0.40, 0.46, 0.56, 0.67 and 0.85, respectively). Bottom left: position–velocity diagram taken along the major axis of the source (PA = 237°; defined by the position angle of the best-fitting ellipse to the CO map), with size and velocity scales shown in the inset. Centre: velocity-coded CO emission, with overlaid MERLIN 1.4 GHz radio contours (white; levels in \(\mu\)Jy beam\(^{-1}\) are 16, 18, 21, 24 and 33). The inset velocity shift legend represents the centre of either the ‘red’ or the ‘blue’ bin, with respect to the centre of the ‘green’ central bin. The CO has been plotted starting at a significance level of 2\(\sigma\) (in the integrated map); all points with detections <2\(\sigma\) have been left black. The radio beam has semimajor and semiminor axes of 0.205 × 0.192 arcsec\(^2\), respectively. The outer contour of the inset ellipse (bottom left) corresponds to the FWHM of the CO beam, which is ∼0.4 arcsec. Velocities are coded relative to the systemic velocity and are shown in the inset. Right: one-dimensional spectra, binned to 40 MHz, taken at the positions indicated. The spectra have been fitted with either single- or double-peaked Gaussian profiles (the fit with the lowest \(\chi^2\) was used in each case).

(NICMOS) 1.6 μm photometry (using the F160W filter) has been added for clarification. There is no ACS image for Lockman 38; instead, we use an I-band image, taken with the CFH12K instrument on the Canada–France–Hawaii Telescope (CFHT). Being ground based, this is necessarily a lower resolution image than the Hubble Space Telescope-ACS photometry, with a resolution of ∼0.7 arcsec.

The middle panels of Figs 1–3 also show the CO data colour coded by velocity. These were created as follows: each data cube has a channel range across which the signal-to-noise ratio (S/N) of the source is maximized. For each source, this channel range was then split into three equal bins, and the CO flux for each point on the map was integrated for each bin separately. This results in three separate maps of the source, corresponding to the three bins in channel space (or three bins in velocity space). These three maps were then colour-coded appropriately and stacked.

The SFR given in Table 2 has been derived using the empirically calibrated far-IR (FIR)–radio correlation, taken from Yun, Reddy & Condon (2001):\(^1\)

\[
L_{\text{FIR}} = 4\pi D_L^2 (8.4 \times 10^{14}) S_{1.4} (1 + z)^{\alpha - 1},
\]

where \(D_L\) is the luminosity distance in metres, \(S_{1.4}\) is the radio flux density at 1.4 GHz (in W m\(^{-2}\) Hz\(^{-1}\)) and \(\alpha\) is the synchrotron slope used to K-correct the 1.4 GHz observations to the appropriate source redshift (\(\alpha\) is taken here to be 0.8). The \(L_{\text{FIR}}\)-SFR conversion was taken from Kennicutt (1998a):

\[
\text{SFR} = 4.5 \times 10^{-44} L_{\text{FIR}} \text{ (erg s}^{-1}\text{).}
\]

It is important to note that several assumptions underlie the direct conversion between \(L_{\text{FIR}}\) and an SFR, namely that all the UV radiation produced by young stars is absorbed by dust and re-radiated in the IR and that the dust heating is brought about by a young stellar population (\(<30\) Myr). If the stellar population is more evolved, the true SFR can be lower than that derived using the above equation by up to a factor of 2.

CO flux densities were estimated by fitting a Gaussian profile to the spectrum. From this, we calculate the CO luminosities using the relation given by Solomon et al. (1997):

\[
L_{\text{CO}} = 3.25 \times 10^{7} S_{\text{CO}} v_{\text{obs}}^{-2} (1 + z)^{-3} D_L^2,
\]

where \(S_{\text{CO}}\) is the CO flux in Jy km s\(^{-1}\), \(v_{\text{obs}}\) is the frequency of the observed CO line in GHz and the luminosity distance \(D_L\) is in Mpc, from which molecular gas masses were derived using a conversion...
Figure 3. Lockman 38. Top left: CO emission contours (yellow), over the CFHT–CFH12K J band (grey-scale). The yellow contours shown in the left-hand panel delineate the 97, 98, 99, 99.5 and 99.9th percentiles of the velocity-integrated CO data (the resultant levels in mJy beam$^{-1}$ are 0.23, 0.26, 0.32, 0.40 and 0.49, respectively). Bottom left: position–velocity diagram taken along the major axis of the source (PA = 193$^\circ$; defined by the position angle of the best-fitting ellipse to the CO map), with the size and velocity scales shown in the inset. Centre: velocity-coded CO emission, with overlaid MERLIN 1.4 GHz radio contours (white; levels in mJy beam$^{-1}$ are 7, 8, 9, 10 and 13). The inset velocity shift legend represents the centre of the ‘red’ or the ‘blue’ bin, with respect to the centre of the ‘green’ central bin. The CO has been plotted starting at a significance level of 2$\sigma$ (in the integrated map); all points with detections <2$\sigma$ have been left black. The radio beam has a radius of 0.5 arcsec. The outer contour of the inset ellipse (bottom left) corresponds to the FWHM of the CO beam, which is $\sim$0.5 arcsec. Velocities are coded relative to the systemic velocity and are shown in the inset. Right: one-dimensional spectra, binned to 40 MHz, taken at the positions indicated. The spectra have been fitted with double-peaked Gaussian profiles.

Table 1. CO properties for HDF 132, HDF 254 and Lockman 38. Note that HDF 132 and Lockman 38 have two entries, for values derived from each of their double peaks.

<table>
<thead>
<tr>
<th>Source</th>
<th>RA [J2000]</th>
<th>Dec. [J2000]</th>
<th>z_{CO} (Jy km s$^{-1}$)</th>
<th>S_{CO} (10^{10} K km s$^{-1}$ pc$^2$)</th>
<th>L_{CO} (10^{10} K km s$^{-1}$ pc$^2$)</th>
<th>L_{CO(1-0)} (10^{10} K km s$^{-1}$ pc$^2$)</th>
<th>M(H$_2$)$^a$ (10$^9$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HDF 132</td>
<td>12:36:18.337</td>
<td>62:15:50.45</td>
<td>1.996</td>
<td>0.77 ± 0.12</td>
<td>0.94 ± 0.14</td>
<td>0.59 ± 0.11</td>
<td>7.2 ± 1.5</td>
</tr>
<tr>
<td>HDF 254</td>
<td>12:37:11.354</td>
<td>62:13:30.90</td>
<td>1.996</td>
<td>0.50 ± 0.08</td>
<td>0.65 ± 0.09</td>
<td>0.40 ± 0.07</td>
<td>8.3 ± 1.7</td>
</tr>
<tr>
<td>Lockman 38</td>
<td>10:53:07.100</td>
<td>57:24:31.87</td>
<td>1.523</td>
<td>0.51 ± 0.07</td>
<td>0.68 ± 0.49</td>
<td>0.53 ± 0.36</td>
<td>8.0 ± 3.9</td>
</tr>
</tbody>
</table>

$^a$H$_2$ masses derived from compact-configuration data, to avoid resolving out flux.

Table 2. Other properties for HDF 132, HDF 254 and Lockman 38. Note that FIR luminosities and SFRs are derived from the 1.4 GHz radio flux densities. Note also that the SFR for HDF 254 has been corrected for AGN contamination, as described in Section 3.2. The 1.4 GHz radio fluxes were obtained by Morrison et al. (in preparation).

<table>
<thead>
<tr>
<th>Source</th>
<th>S_{CO} (mJy)</th>
<th>S_{1.4} (mJy)</th>
<th>L (FIR) (10^{12} L_{\odot})</th>
<th>SFR (FIR) (M_{\odot} yr$^{-1}$)</th>
<th>log $\Sigma_{SFR}$ (M_{\odot} yr$^{-1}$ kpc$^{-2}$)</th>
<th>CO size (radii) (a x b arcsec$^2$)</th>
<th>1.4 GHz size (radii) (a x b arcsec$^2$)</th>
<th>$M_{dyn}$ (10^{10} M_{\odot})</th>
</tr>
</thead>
<tbody>
<tr>
<td>HDF 132</td>
<td>7.3 ± 1.1</td>
<td>172 ± 8.4</td>
<td>8.6 ± 0.6</td>
<td>1500 ± 100</td>
<td>2.19</td>
<td>0.39 ± 0.24 arcsec$^2$</td>
<td>0.24 ± 0.18 arcsec$^2$</td>
<td>21.8 ± 1.8</td>
</tr>
<tr>
<td>HDF 254</td>
<td>2.5 ± 1.2</td>
<td>126 ± 8.7</td>
<td>6.5 ± 0.8</td>
<td>1050 ± 90</td>
<td>1.76</td>
<td>0.52 ± 0.16 arcsec$^2$</td>
<td>0.41 ± 0.14 arcsec$^2$</td>
<td>9.6 ± 0.5</td>
</tr>
<tr>
<td>Lockman 38</td>
<td>6.5 ± 1.9</td>
<td>56.2 ± 22.4</td>
<td>1.5 ± 0.6</td>
<td>250 ± 80</td>
<td>1.13</td>
<td>0.56 ± 0.31 arcsec$^2$</td>
<td>0.29 ± 0.25 arcsec$^2$</td>
<td>6.2 ± 1.1</td>
</tr>
</tbody>
</table>
factor appropriate to local ULIRGs of $X = 0.8 M_\odot K \text{ km s}^{-1} \text{ pc}^2$ (see Tacconi et al. 2008 for discussion).

These molecular gas masses have been derived from CO luminosities resulting from moderate-excitation transitions (either $4 \rightarrow 3$ or $3 \rightarrow 2$); the extrapolation of an accurate gas mass therefore requires a derivation of a CO $(1 \rightarrow 0)$ flux density. We use the brightness temperature conversions derived from SED modelling of SMGs by Weiss et al. (2007), which lead to the following line ratios (as reported by Casey et al. 2009c): $S_{\text{CO}3-2}/S_{\text{CO}1-0} = 7.0 \pm 0.5$; $S_{\text{CO}4-3}/S_{\text{CO}1-0} = 10.0 \pm 0.8$. Most ULIRGs are thermalized up to at least the CO $(3 \rightarrow 2)$ transition, so using these mid-excitation lines ($J_{\text{upper}} = 3$ or 4) should not significantly reduce the extent of the CO emission region when compared to observations of CO $(1 \rightarrow 0)$.

Any size difference will be due to the fact that the higher order transitions trace the actively star-forming gas (which is of interest to us) whereas the lower transitions trace the cold gas either in the outer halo or accreting on to the galaxy.

Use of the long-baseline ‘A’ configuration will inevitably resolve out flux when compared to observations made with more compact configurations. For HDF 132 and HDF 254 we compare our gas masses derived from our observations to those derived using the PdBI ‘D’ configuration, to get an estimate of how much flux has been lost, which is typically a factor of $\sim 2$. For Lockman 38, which has not been observed in ‘D’ configuration, we estimate a true gas mass based on the mean flux lost for the other two sources. We use the (more complete) ‘D’ configuration-derived gas masses when calculating gas surface densities for all systems.

3 RESULTS

3.1 HDF 132

HDF 132 is both the brightest of our three sources at millimetre wavelengths and the most highly obscured (being virtually undetected in the optical), implying an extremely high column density of dust. However, it is detected in the IR [as evidenced by the NICMOS F160W imaging, which was obtained by Conseilie et al. (2008) as part of PID 11082] and is sub-mm bright, with a SCUBA 850 $\mu$m flux of 7.3 $\pm$ 1.1 mJy. The strong 1.4 GHz continuum luminosity implies a high rate of extinction-corrected star formation. This is calculated (from the radio continuum, using the methods described above) to be $1500 \pm 100 M_\odot$ yr$^{-1}$ (here and throughout, quoted errors on the SFR represent fractional errors in the measured radio flux density and do not take into account other uncertainties, e.g. scatter in the $L_{\text{FIR}}$–radio correlation). The velocity-coded image in the centre of Fig. 1 shows what appears to be either a disc-type structure or a late-stage merger.

Spectra taken at separate points along the source (see positional arrows in Fig. 1) reveal the CO spectrum to be double peaked at all points, with the relative intensity of the peaks varying along the axis of the source. [The spectra have been more coarsely binned to 40 MHz ($\sim 76$ km s$^{-1}$) for clarity.] This could possibly be indicative of a ‘beam smearing’ effect, whereby the size of the beam (see the inset ellipse) causes both velocity components to be detected. However, the position in the velocity space of each peak is approximately constant across the galaxy, with just their respective strengths varying. This, coupled with the relatively small beam size (0.4 arcsec – smaller than the source), suggests that the two peaks may be components of line-of-sight rotation.

The position–velocity diagram (Fig. 1, bottom left) shows evidence for ordered gas motion, with two distinct clumps separated in velocity space. While they do overlap in physical space they are offset somewhat (resulting in the two peaks changing in intensity along the axis); this not only could be a signature of rotation (e.g. Funes et al. 2002), but also may be indicative of a late-stage merger.

Fig. 4 shows the kinematics of HDF 132 in more detail. Data were taken along the major axis of the source at $\sim 0.15$ arcsec intervals (or $\sim 1/3$–$1/2$ of the beam FWHM). The bottom panel shows the velocity at each point, obtained by fitting Gaussian curves to each peak of the source. To reach the final mean value for the velocity spread, the positions of the two peaks were weighed by their respective strengths. It is likely that the value of the velocity shear obtained in this manner underestimates the true value, as beam smearing effects cause there to be significant emission from both
components at most points. A better estimate for the true \(v_d\) would be \(\Delta v/2\), where \(\Delta v\) is the separation of the two peaks in velocity space. For HDF 132, \(\Delta v/2 = 288 \pm 19\) km s\(^{-1}\).

The middle panel of Fig. 4 shows the velocity dispersion at each point, taken to be the 1σ value of the Gaussian fit to the peak. The ‘red’ and ‘blue’-shifted peaks have been treated separately, and are coloured red and blue respectively. The top panel compares the CO and the 1.4 GHz flux densities at each point. The small size of the source (\(D < 1\) arcsec) only allows for four points to be taken with enough S/N to allow robust spectra to be taken. This precludes the full elucidation of the velocity behaviour that would be able to characterize the source as either a rotating disc or a merger. However, using the velocity dispersion (Fig. 4, middle panel) it is possible to estimate the lower limit on \(v_d/\sigma\) (see Genzel et al. 2008), a simple way of characterizing the system as either ‘rotation-dominated’ (\(v_d/\sigma > 2–3\)) or ‘dispersion-dominated’ (\(v_d/\sigma < 1\)). The mean velocity dispersions are 113 ± 19 and 157 ± 32 km s\(^{-1}\) for the red and blue components, respectively, leading to a \(v_d(\sin i)/\sigma = 2.03 \pm 0.26\). This is, to first order, comparable to the value claimed for other high-redshift star-forming discs (e.g. Förster Schreiber et al. 2006; Genzel et al. 2006; Law et al. 2007).

Given the fact that it is not apparently dispersion-dominated and that it is homogeneous, compact and non-clumpy on scales of \(<0.5\) arcsec, we identify HDF 132 as a disc-type structure, as opposed to an early-stage major merger (although, of course, a late-stage major-merger remnant is very difficult to distinguish from a true secular disc given the limitations of our observations).

The top panel of Fig. 4 shows a spatial breakdown of the CO and 1.4 GHz distributions. The two trace each other closely, both being centrally peaked and concentrated most strongly over \(<0.5\) arcsec and reaching a maximum value at the same point. The radio continuum emission peaks more strongly, however, falling off more sharply than the CO emission either side of the central peak. Based on its CO morphology, we assign a source size (based on the CO emission half-light radius) of 0.39 × 0.24 arcsec\(^2\) = 3.3 × 2.0 kpc\(^2\) at \(z = 1.996\).

The long-baseline ‘A’ configuration observations often resolve out CO flux when compared to a lower resolution observation (such as the one made in compact ‘D’ configuration with the PdBI). To ensure that we deal with accurate gas surface densities, we take the source size from the high-resolution observations as described above and the total gas mass from low-resolution (compact configuration) observations. The total gas mass for HDF 132 is 7.2 × 10\(^8\) M\(_\odot\) (from as-yet unpublished PdBI observations).\(^2\) This leads to a gas surface density (taking the total gas mass from a mean of the two component peaks) of \(\Sigma_{H_2} = 540\) M\(_\odot\) pc\(^{-2}\). To compare, the star-forming region (\(R_{1/2}\) derived from the radio source extent) is 0.24 × 0.18 arcsec\(^2\). The star formation surface density based on the FIR-inferred SFR is therefore \(\Sigma_{SFR} = 150\) M\(_\odot\) yr\(^{-1}\) kpc\(^{-2}\).

Given that we have identified HDF 132 as a disc-type structure, we can use a simple disc rotation model to calculate its dynamical mass: given its radius of 3.52 kpc and peak-to-peak rotation velocity of 288 ± 19 km s\(^{-1}\), we calculate a dynamical mass of \(M_{\text{dyn}} \sin^2 i = 5.5 \pm 0.5 \times 10^{10}\) M\(_\odot\) (it is important to note that this assumes that the gas is undergoing Keplerian motion). Adopting a fiducial inclination angle of 30°, we find the dynamical mass to be \(M_{\text{dyn}} = 2.2 \pm 0.2 \times 10^{11}\) M\(_\odot\).

### 3.2 HDF 254

HDF 254 is the second brightest (in the radio) of the three sources surveyed. It is also the most extended of the sources, having \(>0.5\) mJy CO emission extended over nearly 1.5 arcsec (= 12.6 kpc at \(z = 1.999\)). It broadly consists of two ‘knots’ of CO emission: a ‘northern’ knot to the north-east and a ‘southern’ knot to the south-west. In addition, there is a slightly weaker CO emission component \(~0.5\) arcsec to the west of the southern knot, with a CO flux of 0.67 mJy – this is a strong MERLIN point source (with a peak 1.4 GHz brightness of \(~3\) μJy beam\(^{-1}\)), which suggests the presence of an AGN. However, both the Hα/NIR observations of Swinbank et al. (2004) and PAH features in the NIR spectra taken by Pope et al. (2008) show little or no evidence for an AGN. The lower CO knot is detected in the ACS optical image (Fig. 2, top left-hand panel) and also robustly detected in 1.4 GHz continuum (Fig. 2, middle panel), implying a high rate of concomitant star formation. By contrast, the northern knot is undetected optically and has a very weak detection in the 1.4 GHz continuum (although radio continuum emission is detected above the 3σ sensitivity limit of \(~10\) μJy at all points along the source). As the velocity-coded image shows, the two knots are distinct structures in velocity space. Spectra taken across the source show it to be single peaked, with a broad velocity dispersion in the northern knot, and double peaked, with lower velocity dispersions in the southern knot. The middle spectrum of Fig. 2 shows a one-dimensional CO spectrum taken at the position of the MERLIN point source. This shows either continuum emission or a broad peak between \(~1000\) and \(~200\) km s\(^{-1}\) relative to the systemic velocity, at a level of \(~0.75\) Jy km s\(^{-1}\). Integrating the spectrum between these two velocities (where the detection is most robust) gives an S/N of \(~3\).

The SFR, calculated using integrated low-resolution VLA measurements of the radio continuum, is \(1220 \pm 100\) M\(_\odot\) yr\(^{-1}\). This is possibly somewhat overestimated, however, as the low resolution of the VLA will include the contribution of the possible AGN to the radio flux, artificially boosting the apparent SFR by up to \(~1/3\) – if the western unresolved MERLIN radio knot is indeed due to an AGN, as expected from the strong hard X-ray emission. Casey et al. (2009b) report a corrected SFR of 1050 M\(_\odot\) yr\(^{-1}\), which we take to be the true SFR hereafter.

Fig. 5 shows a kinematic breakdown for HDF 254. All parameters were derived as for HDF 132 above. The observed velocity shear of \(\pm 80\) ± 28 km s\(^{-1}\) (although again this is a lower limit due to uncertainty in the source inclination) was obtained by fitting a single-peaked Gaussian profile to the CO emission at points along the major axis of the source. As with HDF 132, this method can drastically underestimate the true velocity shear across the system, and in the case of a merging pair it may have little physical interpretation (aside from shedding light on the line-of-sight component of their predominantly transverse velocities). The velocity profile (Fig. 5, bottom panel) resembles a rotation curve, but it may be that the low spatial resolution (\(~4\) kpc beam size) of our observations is inadequate to resolve the characteristic signature of a merging pair of bodies. Both the clumpy (non-disc-like) structure apparent in Fig. 2 and the fact that the CO morphology changes from being

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and four of the peaks positionally trace the CO emission. It is, however, much more highly concentrated in the southern or double-peaked knot, as Fig. 2 shows. The top panel of Fig. 5 shows this in more detail: while the southern component (right-hand peak) is traced very closely by a peak in the radio continuum (with the small 0.1 arcsec offset attributable to astrometrical errors), the northern component (left-hand peak) has very little concomitant star formation.

HDF 254 has a high velocity dispersion, with the mean value of $\sigma$ being $249 \pm 18$ km s$^{-1}$. This is far higher than the likely value of $\sigma_{\text{rot}}$, in as much as a value of $\sigma_{\text{rot}}$ can be placed on such a chaotic system. Examining only the southern knot (which due to its double-peaked CO spectrum appears to have a rotational component), the value of $\Delta v/2$ is $149 \pm 12$ km s$^{-1}$, leading to a $(v_d \sin i)/\sigma$ of 0.67 $\pm$ 0.11, implying that the southern knot is dispersion dominated, and this likely to be undergoing a major merger. While the northern knot is single peaked, and thus has an undefined rotational velocity, its velocity dispersion is high enough, at 285 $\pm$ 25 km s$^{-1}$, to say with some confidence that the northern component too is dispersion-dominated.

Treating the two knots separately, it is possible to estimate the mass of the system. The northern knot is a single-peaked source and as such, using the peak-to-peak velocity shift as a measure of the Keplerian rotation is not viable. Instead, we adopt a velocity-dispersion approach, as in Erb et al. (2006a), whereby

$$M_{\text{dyn}} = \frac{C \sigma^2 r}{G} \quad (4)$$

with the factor $C$ being 3.4 for a rotating disc at an average inclination angle and 5 for a sphere (see e.g. Erb et al. 2006a).

The mean velocity dispersion of the northern knot region is $264 \pm 24.8$ km s$^{-1}$. Assuming a $C$ value of 4 (the body is most likely to be undergoing a major merger. While the northern knot is single peaked, and thus has an undefined rotational velocity, its velocity dispersion is high enough, at 285 $\pm$ 25 km s$^{-1}$, to say with some confidence that the northern component too is dispersion-dominated.

As explained above, the southern knot has a significant line-of-sight rotation component, so it is possible to model the component assuming Keplerian motion. The knot has a radius of 0.2 arcsec, which combined with the above rotational velocity gives a dynamical mass for the lower knot of $M_{\text{dyn, lower knot}} = 5.6 \pm 0.3 \times 10^6 M_\odot$ or, using the fiducial inclination of 30$^\circ$ as above, $M_{\text{dyn}} = 2.2 \pm 0.2 \times 10^6 M_\odot$. For comparison, it is possible to fit a single Gaussian profile to the spectra and derive the dynamical mass using the velocity dispersion as above. Doing so (the mean velocity dispersion in the lower knot is 201 $\pm$ 15 km s$^{-1}$), and adopting a ‘disc’ $C$ value of 3.4, gives a dynamical mass of $M_{\text{dyn}} = 3.1 \pm 0.2 \times 10^6 M_\odot$. This is comparable (within a factor of 2) to the value derived using the peak-to-peak shift: the difference may be due to the poor fitting and artificial broadening of the single Gaussian profile fit to the double-peaked spectrum. The total dynamical mass of the entire system therefore is $M_{\text{dyn}} = 9.6 \pm 0.5 \times 10^6 M_\odot$. The dynamical masses of the separate components clearly mark the system as undergoing a major merger, with a mass ratio of $(2.2-3.1):1$.

To calculate surface densities, we integrate values across the surface of the entire elongated body of the source. As for HDF 132, we take the total gas mass from a low-resolution observation of the same source, to avoid resolving out flux. Casey et al. (2009c) report the total gas mass of this source to be $8.3 \times 10^4 M_\odot$, suggesting that our high-resolution observations resolve out a factor of 2 in CO flux. Based on the CO morphology, we assign source semimajor and semiminor axes (measured using the half-light radius as explained above) of $0.52 \times 0.16$ arcsec$^2$, which leads to a gas surface density
value of $\Sigma_{H_2} = 513 \, M_\odot \, pc^{-2}$. Adopting an identical method for the star formation surface area, we fit the radio emission area with semimajor and semiminor axes of $0.41 \times 0.14$ arcsec$^2$. This gives an SFR surface density of $\Sigma_{SFR} = 58 \, M_\odot \, yr^{-1} \, kpc^{-2}$.

### 3.3 Lockman 38

Lockman 38 is the weakest radio source in our sample, suggesting that it represents an example of the extreme radio-faint end of the SMG population, having an SFR typical of the faintest 20 per cent of SMGs as presented by Ivison et al. (2007). This is similar to the brightest BX/BzK galaxies at $z \sim 1.5$.

The CO emission is moderately extended in the north–south direction, with the strongest emission coming from an elliptical region 1.1 arcsec in diameter, 9.3 kpc at $z = 1.523$. It is comprised of two main velocity components: a small blueshifted region to the north and a larger (and brighter) redshifted region to the south. As with HDF 132, there is a fainter (by a factor of $\sim 2$) ‘tail’ emission component, with a velocity intermediate between the two ‘main’ regions. One-dimensional spectra taken at positions along the source show it to be double peaked at all points. As with HDF 132, the position of each respective peak is close to constant, with the position of the redshifted peak varying by $\pm 33$ km s$^{-1}$ along the source and the position of the ‘blue’ peak varying by $\pm 38$ km s$^{-1}$. Unlike HDF 132, however, the peaks are highly asymmetric, with the redshifted peak near $v \sim 0$ km s$^{-1}$ being around a factor of 5 brighter than the blueshifted peak at $-400$ km s$^{-1}$.

The position–velocity diagram shows the gas motion to be somewhat disturbed. While there is no evidence for spatially separated bodies, there are two distinct kinematic components, which are separated by $v \sim -400$ km s$^{-1}$ in velocity space. These peaks are asymmetric (as discussed above) and do not display the signature of a disc component. The position–velocity diagram suggests that a late-stage merger interpretation of Lockman 38 might be most appropriate, where the components have coalesced to form a single body, but are still kinematically distinct.

The MERLIN+VLA radio continuum map shows the 1.4 GHz emission to be strongly peaking within the brightest plane of the galaxy, with little or no detected emission in either the blueshifted region to the north or the fainter tail. A spatial breakdown of this (Fig. 6, top panel) shows the radio emission falling below the sensitivity threshold of $10 \, \mu$Jy for all but the inner $\sim 0.3$ arcsec of the source.

A kinematic investigation of the source (Fig. 6) shows it to have the largest velocity gradient of the three sources (bottom panel), having a maximum $v_{rot}$, obtained as above using a weighted mean of both peaks of $164 \pm 24$ km s$^{-1}$. This velocity varies smoothly across the source. Using the peak-to-peak shift ($\Delta v/2$), a better measure of the true maximal rotation velocity $v_{rot} = 229 \pm 28$ km s$^{-1}$. The velocity dispersion for the two separate peaks is shown in Fig. 6. The value of $\sigma$ for both peaks varies along the source, though in opposite directions. The mean values for the dispersion are $79 \pm 22$ and $123 \pm 24$ km s$^{-1}$ for the blueshifted and redshifted peaks, respectively. The value of $v_{rot}(\sin i)/\sigma$ for this source (taking a mean of the two peak dispersions) is $2.3 \pm 0.14$, placing the source very much in the rotation-dominated regime. However, due to the disordered and non-rotational gas motions revealed in the position–velocity diagram, we class this source as a late-stage merger, as it is not dispersion-dominated, and apparently non-clumpy on the scales revealed by our beam, yet it does not seem to behave kinematically as a true disc.

As described in Section 2.3, Lockman 38 has never been observed in the compact configuration required to measure a truly accurate gas mass — we can, however, estimate the true value by assuming that with our high-resolution observations we resolve out a similar fraction to the other sources in our programme. We therefore assume that we lose a factor of 1.9 in flux and adjust our derived gas surface density accordingly.

(Obtained by Ibar et al. 2009) VLA imaging of Lockman 38 reveals a total flux density of $32.3 \pm 7.2$ $\mu$Jy, if the source size is assumed to be identical to that of the beam. However, the source is faintly resolved (vaguely consistent with a bipolar morphology) even by the 3.9 arcsec beam. If the source size is deconstrained, the total flux density is $56.2 \pm 22.4$ $\mu$Jy, which is taken to be the true 1.4 GHz flux hereafter. This large radio extent (resolved by the large
Lockman 38 has an unusually low radio-derived SFR for an SMG, at 250 ± 80 M⊙ yr⁻¹. This is despite having a sub-mm flux of 6.5 ± 1.9 mJy, implying an SFR of ~600 M⊙ yr⁻¹. This low radio/sub-mm ratio is unusual given its redshift and hints at an unusually cold dust temperature for this source. Assuming the SFR (radio) to be correct, we again calculate gas and SF surface densities for the source. Due to the highly asymmetric nature of the peaks, we do not take a ‘mean’ value of L′(CO), but instead use the more significantly detected stronger peak. We fit the significant (R₁/₂) CO emission with an ellipse, with semimajor and semiminor axes of 0.31 and 0.56 arcsec, respectively. This gives a gas surface density (including the estimated factor of 1.9 to account for flux resolved out) of Σ_H₂ = 300 M⊙ pc⁻². The radio continuum emission is more highly concentrated than the CO emission and is well fitted by a 0.29 × 0.25 arcsec² ellipse; using the SFR given in Table 2, we arrive at an SFR surface density of Σ_SFR = 14 M⊙ yr⁻¹ kpc⁻².

To estimate the dynamical mass of Lockman 38, we assume rotational motion and use the peak-to-peak velocity shift as a measure of its maximal rotation velocity; we take the radius to be 0.56 arcsec (= 4.75 kpc) and the rotation velocity as 229 ± 28 km s⁻¹. Assuming Keplerian motion, we calculate the dynamical mass to be M_dyn sin² i = 1.6 ± 0.9 × 10¹⁰ M⊙. Taking the fiducial inclination of 30°, the dynamical mass is calculated to be M_dyn = 6.2 ± 1.1 × 10¹⁰ M⊙.

3.4 HDF 255

HDF 255 falls within the field of view for the HDF 254 observation, being just ~7 arcsec to the south-east. It is, however, undetected by our long-baseline ‘A’ configuration observations, suffering from both resolution-based flux loss in the extended source and primary beam attenuation effects (being off phase centre). Fig. 7 shows 12CO (J = 4→3) observations taken with the low-resolution, compact ‘D’ configuration of the PdBI (obtained for our own pilot observations for this programme), along with stacked b-, v-, i- and z-band optical imaging from the ACS.

HDF 255 has been observed in the radio continuum with both MERLIN and the VLA, so calculating the SFR surface density is possible. The FWHM of the MERLIN+VLA image has an elliptical size of 0.56 × 0.32 arcsec² and the 1.4 GHz flux density observed from the VLA is 53.9 ± 8.1 μJy. K-correcting and applying the radio–FIR correlation (as per equation 1), this gives an SFR of 621 ± 93 M⊙ yr⁻¹, with a resultant SFR surface density of Σ_SFR = 16 M⊙ yr⁻¹ kpc⁻².

The galaxy is well detected in CO (~4.5σ) by the compact configuration, but is poorly detected by the long-baseline observations, suggesting that it is a low surface density source with a large extent which has been driven below the sensitivity threshold by the small beam (0.4 arcsec) of the ‘A’ configuration. The compact-configuration flux for HDF 255 is S_CO = 0.53 ± 0.11 Jy km s⁻¹, which leads to a gas mass of 3.5 ± 0.7 × 10¹⁰ M⊙ (after correction to an L_CO value equivalent as above). This relatively low gas mass, coupled with a source size larger than the ‘A’ configuration beam at 154 GHz, leads to the source being resolved out (we would only detect this were all the flux to be concentrated within a beam size). We assume an approximate (lower limit) CO source radius of 0.6 arcsec, based on the high-resolution radio source size and the extent of the beam. This is a rough approximation at best, however, and should be treated with caution. This leads to a value of Σ_gas ≤ 125 M⊙ pc⁻².

4 DISCUSSION

4.1 Mergers versus discs

It is challenging to distinguish between disc-type structures and late-stage merger remnants at high redshift (e.g. Dasyra et al. 2008; Melbourne et al. 2008). Indeed, SMGs are generally classed as either undergoing a major merger or consisting of a compact rotating merger remnant (Swinbank et al. 2006; Shapiro et al. 2008; Tacconi et al. 2008). In our sample, certainly HDF 254 is a system undergoing an early stage major merger: as explained in Section 3.2, the galaxy appears clumpy on sub-arcsecond scales and has an extremely high velocity dispersion (see Fig. 5), indicative of the chaotic and disordered gas motions created by such a merger.

HDF 132, however, does not appear to be undergoing an early stage merging event; its symmetrical velocity peaks, low velocity dispersion (relative to the rotational velocity) and ordered gas motions lend some credence to the non-merging picture. The NICMOS IR morphology of HDF 132 reveals an elliptical structure, with its major axis coincident (within the astrometrical errors) with the major axis of the CO emission. If we are to class HDF 132
(and potentially Lockman 38) as a system not undergoing a major merger, or consisting of a recent merger remnant, we must be able to place these systems on a valid, cosmologically motivated paradigm of galaxy formation which allows for extreme SFRs and extended disc-like structures to emerge from hot/cold flow accretion-type models.

Recent simulations of giant galaxies at high redshifts of $z \sim 2$ (Davé et al. 2009; Dekel et al. 2009) have suggested that extended CO discs can form entirely secularly, without a major-merging event. In this ‘smooth accretion’ model, the systems formed are ‘harassed’ massive galaxies, which are being rapidly formed by filamentary accretion of material from the intergalactic medium (IGM). They can be pictured as undergoing a series of minor mergers (with dark matter halo ratios of $>$1:10), which are observationally indistinguishable from a smooth-accretion-driven secular evolution.

Narayanan et al. (2009) carried out simulations of the star-forming molecular gas within SMGs, using the a priori assumption that SMGs are merger-driven systems. The velocity field (fig. 6 of their paper) shows, in general, a chaotic and disordered structure at all times apart from a short period ($\sim 0.03$ Gyr) in the late inspiral phase of the merger; a system at this stage is yet to undergo the ‘final coalescence’ into a compact merger remnant. It is this final coalescence that boosts the SFR and 850 $\mu$m flux. This results from an a priori assumption that SMGs are merger-driven systems.

4.2 Size of CO emission regions

Recent work investigating the sizes of massive high-redshift galaxies has shown that some high-$z$ galaxies do, in fact, possess extended morphologies. For example, Mancini et al. (2010) investigated a sample of massive early type galaxies, finding that their optical radii were comparable to the radii of similar mass galaxies in the $z = 0$ Universe, suggesting that the low S/N of massive high-$z$ galaxies causes their half-light radii to be systematically underestimated.

HDF 254, the only unequivocally merging system in our study, is comprised of two or three smaller bodies, each $\sim 2$ kpc in diameter, comparable in extent to the mean size of SMGs identified by (for example) Tacconi et al. (2008). This is the first size measurement for a sub-mm faint ULIRG. However, the total system size is $>12$ kpc, and unlike other comparable mergers from Tacconi et al. (2006, 2008) such as HDF 242 and HDF 0931, there is a ‘bridge’ of CO emission connecting the interacting clumps. Both HDF 132 and Lockman 38, however, have CO spatial extents larger than typically seen in high-resolution studies of SMGs. HDF 132 is the most compact of our sources, but with a diameter of $\sim 0.7$ arcsec ($=5.9$ kpc) is more extended than all but one of the 11 sources presented by Tacconi et al. (2006). Lockman 38 has a diameter of 1.1 arcsec (9.5 kpc at $z = 1.523$). The prevailing paradigm of SMGs being major mergers naturally leads to the conclusion that their molecular gas will be concentrated in a compact nuclear region: tidal torquing induced by the merger drives cold molecular gas into the centre of the galaxy, where it is heated, becomes gravitationally unstable and triggers a starbursting event. This suggests that while systems undergoing major mergers may comprise a part of the SMG population, it is perhaps not exclusively so.

4.3 The $L'_\text{CO}$–$L'_\text{FIR}$ relation and star formation efficiency

A common way to conceptualize the relationship between the gas content and SFR of a galaxy is in terms of a star formation efficiency, defined as the SFR per unit of star-forming gas – i.e. SFR/$M(H_2)$. Measuring this for high-$z$ galaxies requires an assumption of a CO–$H_2$ conversion factor; while this is a necessary evil for calculating gas masses and gas surface densities, it is possible to frame the star formation efficiency in terms of observables (assuming the FIR–radio correlation) and use the continuum-to-line luminosity ratio $L'_{\text{FIR}}/L'_\text{CO}$.

We have examined this continuum-to-line luminosity ratio for three ‘sub-regions’ of each of our sources, to better show the star-forming behaviour within each. Fig. 8 shows the result for each of the galaxies. For comparison, other global values of $L'_{\text{FIR}}/L'_\text{CO}$ for SMGs in the literature have been plotted – see the caption for references. All the sub-clumps (by a factor of $\sim 5$) around the canonical $L'_{\text{FIR}}/L'_\text{CO}$ relation as defined by Greve et al. (2005). This relation has a slope less than unity, indicating that as $L'_{\text{FIR}}$ increases, so does the $L'_{\text{FIR}}/L'_\text{CO}$ ratio: star formation is more efficient in ultraluminous systems such as SMGs than in LIRGS and normal star-forming galaxies. However, Krumholz & McKee (2005) have suggested that it is not a star formation efficiency issue, but rather results from a disconnection between the gas being traced and the gas actively involved in star formation (see e.g. Gao et al. 2007). In this picture, CO emission with $J_{\text{upper}} \leq 4$ traces the ambient gas density (which is non-linear with the SFR), whereas emission from

\[
\begin{align*}
\text{Figure 8. CO luminosity plotted against the FIR luminosity for } \text{sub-clumps of our three sources. For reference, results for other SMGs in} \\
\text{the literature have been plotted (Downes & Solomon 2003; Genzel et al.} \\
\text{2003; Neri et al. 2003; Sheth et al. 2004; Greve et al. 2005; Daddi et al.} \\
\text{2009; Knudsen et al. 2009). The dashed line represents the fit to SMGs and} \\
\text{ULIRGs from Greve et al. (2005) of } \{\log L'_\text{CO} = 0.62(\log L'_{\text{FIR}}) + 2.33\}. \\
\text{All our sources scatter around the canonical relation by up to a factor of 5.}
\end{align*}
\]
molecules that trace the densest star-forming cores (such as HCN) is better suited for measuring the density of the gas actually involved in star formation. Indeed, in the local Universe L(HCN) is seen to increase linearly with L(FIR). The sub-clumps of our three SMGs follow this (non-linear) trend and have $L_{\text{FIR}}/L_{\text{CO}}$ ratios consistent with other SMGs. As can be seen from Fig. 8, Lockman 38 is the least-efficient SMG studied to date, further suggesting that it is a highly unusual system.

4.4 Gas fractions and the uncertain CO conversion factor

The question of the appropriate CO/H$_2$ conversion factor to use in extreme high-$z$ systems is an ongoing one. The generally accepted values for local ULIRGs are within the range 0.8–1.6 $M_\odot$ K km s$^{-1}$ pc$^2$, substantially lower than the calibration used for ‘normal’ systems – this value (normally referred to as the Milky Way, or galactic, conversion factor) is generally taken to be 4–5 $M_\odot$ K km s$^{-1}$ pc$^2$ and is derived both theoretically and empirically (see appendix A of Tacconi et al. 2008 and references therein for discussion). Obtaining the correct value for any given system is difficult, however, as the true value is a complex function of many physical parameters, including the gas metallically (Israel 2005), and the column density and temperature of the interstellar gas (Sakamoto 1996; Weiß et al. 2001; Wall 2007).

The theoretical justification for using a significantly lower conversion factor for ULIRGs than normal star-forming galaxies hinges on the nature of merger-induced star formation. Whereas ‘normal’ star formation occurs in gravitationally bound molecular clouds (which exist as well-defined separate structures in the ISM), the torque induced by a merger event creates a more centralized, homogeneous molecular ISM, in which pressure plays a significant role in triggering a star-forming event. This difference (gravitationally confined versus pressure-confined star-forming gas) theoretically justifies the use of a different conversion factor. Empirically, it is found that using a standard galactic conversion factor for ULIRGs often results in derived gas masses greater than their dynamical masses, necessitating the adoption of a lower value.

The paradigm of SMGs being ‘scaled-up’ versions of local ULIRGs has led to these lower values of $X_{\text{CO}}$ being adopted by most authors (i.e. $X = 0.8$ by Greve et al. 2005; $X = 1$ by Tacconi et al. 2008), which has led to a predominance of low assumed gas fractions for SMGs, which typically have values of $f_{\text{gas}}$ ($= M_{\text{gas}}/M_{\text{dynamical}}$) between 0.1 and 0.3. Fig. 9 shows the relationship between dynamical mass and gas mass for the sources in this work, along with a selection of SMGs from the literature – diagonal lines of constant gas fraction have been drawn for clarity. A majority of the galaxies shown (9/17) have low gas fractions of <20 per cent, a value which would be modest for local star-forming discs (e.g. Karachentsev et al. 2004; Bothwell, Kennicutt & Lee 2009) and seems utterly incongruous with the exceptional SFRs achieved by SMGs.

For the three ULIRGs considered in this paper, we have measured relatively extended CO structures of low gas surface density, comparable to local starburst galaxies and distinctly different from the dense, nucleated gas of local ULIRGs. It is therefore reasonable to consider that the use of the CO conversion factor appropriate for local ULIRGs ($X \sim 1$) might not be justified in the types of systems uncovered in this work. We also show in Fig. 9 (as open red circles) the effect of using a Milky Way conversion factor ($X = 4.3 M_\odot$ K km s$^{-1}$ pc$^2$) for our three galaxies.

A full theoretical and empirical treatment of the CO/H$_2$ conversion factor lies beyond the scope of this work. We do, however, include in the following discussion of the star formation law the possibility that the assumed value of $X = 0.8 M_\odot$ K km s$^{-1}$ pc$^2$ may be significantly underestimating the true gas mass.

4.5 The star formation law

There have been many recent studies on star formation at high redshifts, putting the extreme systems seen at $z > 2$ (where the cosmic SFR density peaks) in the context of a ‘universal star formation law’. The most common prescription, at both low and high redshifts, is the power-law scaling between the surface density of gas ($\Sigma_{\text{gas}}$) and star formation ($\Sigma_{\text{SFR}}$) known as the KS law (Schmidt 1959; Kennicutt 1998b).

A full and correct calibration of the high-$z$ KS law is crucial in order to facilitate studies of star-forming galaxies at cosmological redshifts. With current instrumentation it is only possible to measure CO masses for the most luminous systems: this has the result that all galaxies currently observed in CO at $z > 2$ are ULIRGs, which are clearly unrepresentative of the high-$z$ population as a whole. In addition, obtaining accurate gas masses via CO measurements is highly time consuming, requiring on-source integration times of several hours; as such, obtaining well-constrained gas masses for a statistically significant sample of high-$z$ star-forming galaxies would be prohibitively expensive in terms of instrument time. One way around this is to infer a gas mass based on the (more easily measurable) H$_\alpha$ emission size and SFR (e.g. Erb et al. 2006b). This requires the assumption of a universal star formation law, which has only been truly calibrated at low redshifts and may be inaccurate for both the ‘normal’ ($L^*$ galaxies) and extreme systems (SMGs, SFRGs, etc.) lying at cosmological redshifts. Clearly, for this kind of large-scale work to be undertaken there is a need for.

high-redshift galaxies to be placed in the context of a KS-type star formation law.

Erb et al. (2006b) established a plausible KS-law relation for BX/BM galaxies by inverting the KS law for gas surface densities. Tacconi et al. (2006) explicitly measured the gas surface densities in SMGs and inferred the basic KS-law properties of SMGs, while Bouché et al. (2007) reviewed the literature on this topic and placed all these galaxies in a self-consistent framework, re-iterating the findings of both these authors. Bouché et al. (2007) report that, in general, extreme star-forming galaxies at high redshifts lie above the $z \sim 0$ KS law originally proposed by Kennicutt (1998b), a fact which they attribute to an environmental enhancement of the SFR most likely due to collisions or pressure. When including the high-$z$ galaxies, they modify the canonical KS slope of $N \sim 1.4$, finding that $N = 1.71 \pm 0.05$ provides a better fit. Even taking this steeper relation into account, the SMGs in their study still lie above the relation, indicating the very high efficiency of their star formation. Bouché et al. (2007) were, however, forced to make assumptions, including the fact that the sizes of the CO region and the star-forming region were identical, using the half-light radius ($R_{1/2}$) of the CO emission for both.

Our high-resolution, matched beam study of SMGs allows us to improve over previous studies by taking independent observations of both the sizes of the star-forming and the CO emission regions and by utilizing accurate and independent measures of SFRs and gas masses. As discussed in Section 3 (see Table 2), we find that in all instances the star-forming region is centrally peaked and is extended over a smaller region than the CO morphology. Taking the ‘size’ of the respective emission regions to be the half-light radius, we calculate the surface density of both star formation and molecular gas (which we correct for interstellar helium by multiplying our molecular gas masses by 1.36).

Fig. 10 shows our three sources in the context of the KS law. The smaller size of the 1.4 GHz emission region (respective to the CO emission region) leads to the three sources presented in this work lying significantly above the $z \sim 0$ KS relation and above the high-$z$ ULIRGS previously examined. This indicates an extremely high efficiency of star formation respective to the gas density. Even Lockman 38 – which may be forming stars an order of magnitude slower than a typical SMG (as per the above discussion) – has such an extended CO morphology and compact radio emission that its gas surface density is lower than would be expected given its SFR, causing it to lie above the high-$z$ KS relation. Both HDF 132 and HDF 254 lie significantly ($\sim 0.8$ dex) off the KS slope: it is likely to be a combination of the extended CO morphology and compact radio emission which conspires to move the sources above the relation. As discussed above, however, this finding is dependent on the assumption of a merger-appropriate CO/H$_2$ conversion factor for our sources, which may be significantly underestimating the gas content for our galaxies, particularly the disc-like HDF 132 which has a gas fraction of 5 per cent assuming a ULIRG-appropriate conversion factor. If the smaller conversion factor is rejected and instead a Milky Way factor is used, then our galaxies fall very close to the high-$z$ KS relation of Bouché et al. (2007).

Using our independent measurements of the MERLIN-observed star-forming regions and the CO morphology, we have also recalculated $\Sigma_{\text{gas}}$ and $\Sigma_{\text{SFR}}$ for SMGs from the literature: these properties are presented in Table 3. For consistency, all gas surface densities have been adjusted to a common CO/H$_2$ conversion factor of $0.8 M_\odot \text{K km s}^{-1} \text{pc}^2$ (though an error bar again delineates the possible range of values, up to the standard Milky Way value) and all SMG molecular gas masses have had a helium correction factor of 1.36 applied. These archival SMGs are also shown in Fig. 10. There appears to be an offset between the SMGs presented in this work (both newly observed and archival) and the KS relation for high-$z$ star-forming galaxies claimed by Bouché et al. (2007), which suggests that obtaining an estimate of a galaxy’s gas mass by inverting the canonical KS law can give unreliable results. Furthermore, as explained above the offset between our sources and other suggested KS-law slopes is, perhaps, partly attributable to a combination of uncertainties in the CO/H$_2$ conversion factor and SFRs for this type of system, but could also provide evidence that stars are formed more efficiently in these extreme systems. If this is the case, then it may be that a ‘universal star formation law’, which provides a consistent power-law relationship between gas content and star formation across all systems and environments, is not achievable or at least does not apply in the most extreme cases.

5 CONCLUSIONS

We have presented high-resolution (sub-arcsecond) detections of molecular gas in three $z \sim 2$ star-forming galaxies, two SMGs and one SFRG. We used extracted spectra to constrain CO fluxes, and extrapolated total molecular gas masses. We analysed the kinematic behaviour of the sources revealed in the CO imaging on 0.15 arcsec scales, equal to $\sim 1/3–1/2$ of the beam FWHM. Our main conclusions are as follow.
(i) One of our galaxies is unequivocally an early stage major merger (HDF 254) with high velocity dispersion and a minimal rotational contribution. Lockman 38 appears to be a late-stage merger, with a low velocity dispersion and a smooth morphology, but with significantly disturbed gas kinematics revealed by the position–velocity diagram. The remaining detected source (HDF 132) appears – to the limits of our data – consistent with being a disc-like rotating body, with double-peaked profiles indicative of rotation and a homogeneous, non-clumpy morphology. These features may be explainable with a late-stage merger model or may be evidence of a star-forming disc.

(ii) There is a marked discrepancy between the sizes of the CO and 1.4 GHz radio emission regions in our high-resolution data, with the radio emission region (which traces star formation) being more compact than the CO region in all cases. This has important implications for our understanding of star formation in high-z starburst galaxies, particularly in relation to the role of gas reservoirs, and whether starburst galaxies tend to be fuelled by cold flow accretion, or minor mergers (see Dekel & Birnboim 2006).

(iii) This size difference leads to an exacerbation of the offset of SMGs from the KS star formation law, which has already been shown to be significant (see Bouché et al. 2007 for a compilation of recent findings in this area).

(iv) The adoption of a low, ULIRG-like CO/H$_2$ conversion factor for SMGs leads to very low gas fractions of <30 per cent, which is far lower than would be expected given their extreme SFR. The adoption of a Milky Way conversion factor (which is somewhat theoretically supported) raises the gas mass by a factor of 5.

(v) This size difference also manifests in the form of a star formation efficiency variation, with ‘sub-clumps’ of our sources differing in efficiency by up to a factor of ~5. However, the global properties of each source are consistent with the canonical L$_{CO}$-L$_{SFR}$ relation for similarly extreme (and sub-mm bright) systems.

(vi) These are the first PdBI observed ‘A’ configuration observations of high-z ULIRGs for CO (4$\rightarrow$3), achieving the smallest beam size yet for an intermediate-excitation transition at a redshift of ~2. The modest exposure times required (six antennas equivalent of ~8 h), the small loss of flux (a factor of 1.9 on average), and the detailed morphologies and kinematic information revealed suggest that this is a profitable approach for similar investigations in the future.

<table>
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<th>Source</th>
<th>z</th>
<th>$R_{1/2}$ (CO) (kpc)</th>
<th>$R_{1/2}$ (1.4 GHz) (kpc)</th>
<th>log $\Sigma_{gas}$ (M$_\odot$ pc$^{-2}$)</th>
<th>log $\Sigma_{SFR}$ (M$_\odot$ yr$^{-1}$ kpc$^{-2}$)</th>
<th>MERLIN data reference</th>
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<td>2.73</td>
<td>2.16</td>
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<td>1.99</td>
<td>2.9</td>
<td>2.3</td>
<td>2.71</td>
<td>1.76</td>
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<td>Lockman 38</td>
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<td>2.3</td>
<td>2.48</td>
<td>0.76</td>
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<td>3.2</td>
<td>2.13</td>
<td>1.19</td>
<td>Chapman et al. (2004)</td>
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</table>

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