GRB 050410 and GRB 050412: are they really dark gamma-ray bursts?

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ABSTRACT

Aims. We present a detailed analysis of the prompt and afterglow emission of GRB 050410 and GRB 050412 detected by Swift for which no optical counterpart was observed.

Methods. We analysed data from the prompt emission detected by the Swift BAT and from the early phase of the afterglow obtained by the Swift narrow field instrument XRT.

Results. The 15–150 keV energy distribution of the GRB 050410 prompt emission shows a peak energy at \(53^{+61}_{-21}\) keV. The XRT light curve of this GRB decays as a power law with a slope of \(\alpha = 1.06 \pm 0.04\). The spectrum is well reproduced by an absorbed power law with a spectral index \(\Gamma_1 = 2.4 \pm 0.4\) and a low energy absorption \(N_H = 4.3^{+1.4}_{-0.7} \times 10^{21} \text{cm}^{-2}\) which is higher than the Galactic value. The 15–150 keV prompt emission in GRB 050412 is modelled with a hard (\(\Gamma = 0.7 \pm 0.2\)) power law. The XRT light curve follows a broken power law with the first slope \(\alpha_1 = 0.7 \pm 0.4\), the break time \(t_{\text{break}} = 254^{+119}_{-32} \text{s}\) and the second slope \(\alpha_2 = 2.8^{+0.3}_{-0.7}\). The spectrum is fitted by a power law with spectral index \(\Gamma_2 = 1.3 \pm 0.2\) which is absorbed at low energies by the Galactic column.

Conclusions. The GRB 050410 afterglow light curve reveals the expected characteristics of the third component of the canonical Swift light curve. Conversely, a complex phenomenology was detected in the GRB 050412 because of the presence of the very early break. The light curve in this case can be interpreted as being the last peak of the prompt emission. The two bursts present tight upper limits for the optical emission, however, neither of them can be clearly classified as dark. For GRB 050410, the suppression of the optical afterglow could be attributed to a low density interstellar medium surrounding the burst. For GRB 050412, the evaluation of the darkness is more difficult due to the ambiguity in the extrapolation of the X-ray afterglow light curve.

Key words. gamma rays: bursts – X-rays: bursts – X-rays: individuals: GRB 050410 – X-rays: individuals: GRB 050412

1. Introduction

Gamma-Ray Bursts (GRBs), the brightest explosions in the universe, produce emission across the whole electromagnetic spectrum from γ-rays to radio wavelengths. However, multi-wavelength observations have shown that the optical counterpart following the prompt emission is detected in only about 50% of the well localised events (De Pasquale et al. 2003; Roming et al. 2006; Roming & Mason 2006).

The paucity of optical detections of GRB afterglows has been explained by invoking different mechanisms (Lazzati et al. 2002; Lamb & Reichart 2000; Groot et al. 1998; Taylor et al. 1998; Wijers et al. 1998; Totani 1997). More recently, by comparing the Swift optical, X-ray and γ-ray data sets, Roming et al. (2006) identified a class of optically “dark” GRBs with higher than normal γ-ray efficiency. A possible mechanism proposed for these GRBs is based on a Poynting flux dominated outflow (Zhang & Kobayashi 2005) where the transfer of the energy from the fireball to the medium is delayed, leading to the suppression of the reverse shock, likely responsible for the prompt optical emission, and to an apparent high γ-ray efficiency. A stronger alternative mechanism proposed is a pure non-relativistic hydrodynamical reverse shock (Kobayashi 2000; Nakar & Piran 2004; Beloborodov 2005; Kobayashi et al. 2005; Uhm & Beloborodov 2006; McMahon et al. 2006).

The characterisation of optical darkness has been previously based on the upper limit of the optical/NIR afterglow flux (Rol et al. 2005; Filliatre et al. 2005, 2006) or the optical-to-X-ray spectral index (Jakobsson et al. 2004). In particular, if the optical-to-X-ray spectral index, \(\beta_{\text{ox}}\), is lower than 0.5 the afterglow should be classified as dark; while for Rol et al. (2005) dark afterglows are those with optical upper limits falling below the extrapolation of the X-ray spectrum to the optical range.

The Swift Gamma-Ray Burst Explorer (Gehrels et al. 2004), successfully launched on 2004 November 20, is a multi-wavelength observatory dedicated to the discovery and study
of GRBs and their afterglows. It carries three instruments: the Burst Alert Telescope (BAT; Barthelmy et al. 2005) and the two narrow-field instruments: the X-Ray Telescope (XRT; Burrows et al. 2005) and the Ultra-Violet Optical Telescope (UVOT; Roming et al. 2005b). Swift’s capability of rapidly re-pointing the spacecraft in a few tens of seconds after a BAT detection, allows a study of the first phases of an afterglow evolution over a broad energy range from optical to X-rays.

In this paper, we present the results on the analysis of the prompt and the afterglow emission of GRB 050410 and GRB 050412 observed by Swift, two bursts for which no optical counterpart was detected.

Errors in the paper are relative to a 90% confidence level for a single parameter ($\Delta T_m = 2.71$). Times are referenced from the BAT trigger, $T_0$. The decay and spectral indices are parameterised as follows:

$$F(T,\nu) \propto T^{-\alpha} \nu^{-\beta}$$

where $F(T,\nu)$ (erg cm$^{-2}$ s$^{-1}$ Hz$^{-1}$) is the monochromatic flux as a function of time $T$ and frequency $\nu$; we also use $\Gamma = \beta + 1$ as the photon index $N(E) \propto E^{-\Gamma}$. (ph cm$^{-2}$ s$^{-1}$ keV$^{-1}$) where $N(E)$ is the number of photons at the energy $E$.

2. Observation

GRB 050410 triggered BAT at 12:14:25.36 UT (Fenimore et al. 2005). At the time of the first detection, GRB 050410 was within the Swift Earth-limb constraint, therefore, the observatory executed a delayed automated slew to the BAT position and started observing with the narrow-field instruments ~32 min after the burst. At that time, the X-ray afterglow was too faint for the XRT to produce an on-board centroid, therefore a position was determined during ground processing (La Parola et al. 2005). No new source was detected by UVOT within the BAT and XRT error circle with the magnitude of $R = 19.9, B = 21.2$ and $U = 20.9$ (Boyd et al. 2005). Ground based follow-up also did not detect any optical counterpart for GRB 050410 down to a limiting magnitude of $V = 20.5$ at times after the burst of $T = 13.3$ ks (Misra et al. 2005), $T = 17.5$ ks (Ofek & Lipkin 2005) and $T = 20.6$ ks (Runyan et al. 2005); and limiting magnitudes of Gunn $i = 21.5$ and Gunn $z = 20.0$ at $T = 56.2$ ks after the burst (Cenko & Fox 2005a). No radio counterpart was detected down to $2\sigma$ upper limit of 114 mJy (Soderberg 2005a).

The second burst considered in the paper, GRB 050412, was discovered by Swift at 05:44:03 UT (Cummings et al. 2005; Tueller et al. 2005). The observatory executed an automated slew to the BAT position and the XRT and UVOT began taking data 99 s after the BAT trigger. The position of the X-ray counterpart was derived from the first orbit of data and was given in Mangano et al. (2005). UVOT data revealed no evidence of a fading source in the $5^\prime'$ radius XRT error circle; the 3$\sigma$ limiting magnitude was $V = 19.1$ (Roming et al. 2005a). The Chandra X-ray Observatory observed GRB 050412 with the ACIS for 20 ks on 2005 April 17, when the source was no longer visible in the XRT data. No X-ray source was detected by Chandra and an upper limit on the unabsorbed 0.5–10 keV flux of $3.6 \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$ was inferred (Berger & Fox 2005).

Table 1. Observation log for the data used in the analysis of GRB 050510 and GRB 050512.

<table>
<thead>
<tr>
<th>Obs. #</th>
<th>Start time (UT)</th>
<th>Exposure (yyyy-mm-dd hh:mm:ss)</th>
<th>WT(s)</th>
<th>PC(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>GRB 050410</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>2005-04-10 12:46:24</td>
<td>9436</td>
<td>8635</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>2005-04-12 16:15:47</td>
<td>–</td>
<td>4740</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>2005-04-12 00:11:47</td>
<td>–</td>
<td>1473</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>2005-04-14 00:22:44</td>
<td>–</td>
<td>3184</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>2005-04-15 00:30:44</td>
<td>–</td>
<td>10895</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>2005-04-16 00:32:01</td>
<td>–</td>
<td>13086</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>2005-04-17 16:45:01</td>
<td>–</td>
<td>6418</td>
<td></td>
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<tr>
<td>8</td>
<td>2005-04-19 00:50:42</td>
<td>–</td>
<td>9832</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>2005-04-20 00:54:29</td>
<td>–</td>
<td>11123</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>2005-04-21 00:55:58</td>
<td>–</td>
<td>1828</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Total exposure(s)</td>
<td>9436</td>
<td>71214</td>
<td></td>
</tr>
<tr>
<td>GRB 050412</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>2005-04-12 05:45:47</td>
<td>3019</td>
<td>1950</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>2005-04-14 00:04:59</td>
<td>–</td>
<td>3719</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>2005-04-17 09:28:35</td>
<td>–</td>
<td>6200</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Total exposure(s)</td>
<td>3019</td>
<td>11869</td>
<td></td>
</tr>
</tbody>
</table>

3. BAT and XRT data reduction and analysis

The BAT event data were re-analysed using the standard analysis software\(^1\) included in the HEASoft 6.0.4 package. Response matrices were generated with the task BATDRMGEN using the latest spectral redistribution matrices. The BAT background was subtracted using a mask-weighting technique that is only effective up to 150 keV.

XRT data were calibrated, filtered and screened with the XRTDAS software package, included in the HEAsoft 6.0.4 package, to produce cleaned photon list files. Only time intervals with the CCD temperature below $-47$ C$^\circ$ were selected. Table 1 shows the observation log for GRB 050510 and GRB 050512.

Standard grade selection, 0–12 for Photon Counting (PC) mode and 0–2 for Window Timing (WT) mode (Hill et al. 2004), was used for both spectral and timing analysis. Ancillary response files for PC and WT spectra were generated with the standard XRTPKarf tool (v 0.5.1) using calibration files from CALDBv2.3.

WT data were extracted in a rectangular region 40 $\times$ 20 pixels along the image strip which included about 96% of the Point Spread Function (PSF). PC data were extracted from a circular region of 20 pixels radius for observing intervals with a rate lower than 0.2 counts s$^{-1}$. In time periods with higher rates, the extraction region used was an annulus with an inner radius of 3 pixels and an outer radius of 20 pixels in order to take into account pile-up effects. The two regions included, assuming an average energy of 1.5 keV, 92% (circular) and 48% (annulus) of the PSF, respectively. The WT and PC backgrounds were extracted from regions far from the GRB counterpart and from any sources in the field. WT and PC spectral analysis of both GRBs was performed in the energy range 0.7–10 keV to avoid residual

\(^1\) see http://swift.gsfc.nasa.gov/docs/swift/
Table 2. Best fit parameters for the spectral analysis in the energy ranges 15–150 keV (BAT) and 0.7–10 keV (XRT) for GRB 050410 and GRB 050412.

<table>
<thead>
<tr>
<th></th>
<th>GRB 050410</th>
<th>GRB 050412</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Power Law</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Gamma$</td>
<td>1.66 ± 0.07</td>
<td>0.7 ± 0.2</td>
</tr>
<tr>
<td>$\chi^2$ (d.o.f.)</td>
<td>1.67 (36)</td>
<td>0.55 (15)</td>
</tr>
<tr>
<td><strong>Band Model with $\beta_{\text{Band}} = -2.3$</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_{\text{Band}}$</td>
<td>-0.79 ± 0.09</td>
<td>-</td>
</tr>
<tr>
<td>$E_p$ (keV)</td>
<td>53 (41)</td>
<td>-</td>
</tr>
<tr>
<td>$\chi^2$ (d.o.f.)</td>
<td>1.11 (35)</td>
<td>-</td>
</tr>
<tr>
<td><strong>Cut-off Power Law</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_{\text{cut-off}}$</td>
<td>-0.8 ± 0.3</td>
<td>-</td>
</tr>
<tr>
<td>$E_p$ (keV)</td>
<td>54 (11)</td>
<td>-</td>
</tr>
<tr>
<td>$\chi^2$ (d.o.f.)</td>
<td>1.08 (35)</td>
<td>-</td>
</tr>
<tr>
<td><strong>Power Law</strong></td>
<td>0.7–10 keV (XRT)</td>
<td></td>
</tr>
<tr>
<td>$N_{\text{fit}}$ (cm$^{-2}$)</td>
<td>$4^{+3}_{-6} \times 10^{21}$</td>
<td>$2.21 \times 10^{20}$</td>
</tr>
<tr>
<td>$\Gamma_s$</td>
<td>2.4 ± 0.4</td>
<td>1.3 ± 0.2</td>
</tr>
<tr>
<td>$\chi^2$ (d.o.f.)</td>
<td>0.64 (13)</td>
<td>1.18 (17)</td>
</tr>
</tbody>
</table>

background due to bright Earth contamination and dark current that are more dominant at lower energies.

3.1. GRB 050410

GRB 050410 triggered Swift twice as a result of an anomalous time-out of the triggering code (Fenimore et al. 2005). In our analysis, we consider as reference time the time of the first trigger ($T_0 = 12:14:25.36$ UT).

The 15–150 keV light curve of the prompt emission, shown in Fig. 1, is characterised by a broad peak with $T_{90} = 44 \pm 1$ s. The burst shape can be modelled by two Gaussians of the same width (11 ± 2 s), the first centered at 5 ± 1 s and the second at 32 ± 2 s.

The 15–150 keV energy distribution of the burst, modelled with a simple power law of photon index $\Gamma = 1.66 \pm 0.07$, gave a marginally acceptable fit with $\chi^2_{\text{red}}$ of 1.67 for 36 d.o.f. (see Table 2). Better fits were obtained using a cut-off power law or a Band model (Band et al. 1993) with the high energy photon index, $\beta_{\text{Band}}$, fixed to $-2.3$ according to the expected value (Preece et al. 2000). The best fit values of the spectral parameters are shown in Table 2. The improvement with respect to the power law fit is significant for both models, with a chance random probability of $\sim 7 \times 10^{-5}$, assuming that the errors are normally distributed. The fluence in the 15–150 keV energy range was $(4.6 \pm 0.1) \times 10^{-6}$ erg cm$^{-2}$.

The XRT observed GRB 050410 for 10 orbits for a total exposure of $\sim 9$ ks in WT mode and $\sim 71$ ks in PC mode. The position of the burst, determined with astrometry solutions, was RA$_{2000} = 05^h 59^m 13^s 94$ Dec$_{2000} = +79^\circ 36' 11" 7$, with an uncertainty of 2'3 (Butler 2007). These coordinates lie outside the error circle (3''7 radius) of the position derived with the tool XRTCENTROID and 42'' from the BAT position reported by Fenimore et al. (2005).

The GRB 050410 XRT light curve shows a clear decay with time that can be well modelled ($\chi^2_{\text{red}} = 0.87$ with 13 d.o.f.) by a single power law with a slope $\alpha = 1.06 \pm 0.04$. The light curve, shown in Fig. 2, was converted to flux by applying a conversion factor derived from the spectral analysis. The dashed line represents the best fit model. The BAT light curve was extrapolated to the XRT band by converting the BAT count rate with a factor derived from the Band spectral parameters (see Table 2). The vertical line at 13.3 ks indicate the time of the Misra et al. (2005) optical upper limit.

WT and PC spectra were fitted simultaneously because no spectral evolution with time was detected. The two spectra normalisations were left free to vary, thus accounting for the different average flux levels in the two observing periods. An absorbed power law reproduces well the emission ($\chi^2_{\text{red}}$ of 0.64 for 13 d.o.f.) with the best fit parameters (see also Table 2) $\Gamma_s = 2.4 \pm 0.4$ and $N_H = 4^{+3}_{-2} \times 10^{21}$ cm$^{-2}$. Note that the absorbing column is non-zero at the 4-sigma level, and the best-fit value of the absorbing column is $\sim 5$ times larger than the Galactic one (7.53 $\times 10^{20}$ cm$^{-2}$;Dickey & Lockman 1990).

3.2. GRB 050412

The GRB 050412 prompt emission showed a double-peaked structure with the first peak centered at $-1.1 \pm 0.4$ s from the trigger (width of 4.7 $\pm$ 0.6 s), and the second fainter and wider...
(11 ± 3 s) peak centered at 16 ± 5 s (see Fig. 3). The estimated $T_{90}$ in the 15–150 keV energy band was 27 ± 1 s. The hardness ratio (50–150 keV and 15–50 keV) does not show any significant evidence of spectral variation during the burst evolution.

The 15–150 keV energy distribution was well described ($\chi^2_{\text{red}} = 0.55$ for 15 d.o.f.) by a single power law with an hard photon index of $\Gamma = 0.7 ± 0.2$. The $T_{90}$ burst fluence in the 15–150 keV energy range was $(6.3 ± 0.3) \times 10^{-7}$ erg cm$^{-2}$. A Band model and a cut-off power law were not able to reproduce this spectrum because some of the fitting parameters are not constrained.

The XRT detected a rapidly fading source at RA$_{2000} = 12^h 04^m 25^s 2$ Dec$_{2000} = -01^\circ 12^\prime 00^\prime\prime .4$, with an uncertainty of 4.2 s. This position, derived with the tool XRTCENTROID, is 60 s from the BAT position (Tueller et al. 2005) and it is in agreement with the refined value derived with astrometry technique (Butler 2007).

The XRT light curve is not consistent with a single power law ($\chi^2_{\text{red}} = 2.3$ with 18 d.o.f.). A better fit ($\chi^2_{\text{red}} = 0.7$ with 14 d.o.f.) can be obtained with a broken power law whose best fit parameters are: $a_1 = 0.7 ± 0.4$, $a_2 = 2.8_{-0.5}^{+0.6}$ and $T_{\text{break}} = 254_{-41}^{+79}$ s.

The GRB 050412 light curve was converted to the 0.2–10 keV flux with a procedure similar to the one used for GRB 050410, and plotted in Fig. 4 together with the BAT light curve extrapolated to the XRT energy range. In the same figure, the 3σ upper limit obtained by Chandra is also plotted (Berger & Fox 2005).

The upper limits derived from Swift observations 2 (2005-04-14) Dec $\pm 0.5$ was obtained by Chandra. The vertical line at 8.3 ks indicates the time of the Kosugi et al. (2005) optical upper limit.

4. Discussion

The discussion on the results of GRB 050410 and GRB 050412 analysis is based on two main points: (i) the comparison of the X-ray afterglow light curves with other Swift results, particularly important for GRB 050412 where a very early break (~250 s) followed by a steep decay $\alpha_2 = 2.8_{-0.8}^{+0.6}$ were detected; (ii) the classification of the two bursts as dark.

4.1. The X-ray light curve

The X-ray afterglow light curves of many bursts manifest a similar behaviour (O’Brien et al. 2006; Nousek et al. 2006; Willingale et al. 2006). The canonical X-ray light curve has an initial steep decay (usually interpreted as emission from the tail of the prompt GRB), followed by a flatter decay phase that can last up to $10^2$ s (interpreted as a refreshing of the forward shock), and a final steeper decay phase with power law indices consistent with the values measured before the launch of Swift (Frontera 2003). This canonical light curve is consistent with about 60% of the Swift afterglows. In many of the non-conforming cases, the first, or the first and the second branches are missing. The lack of detection of these portions of the light curve cannot always be attributed to missing observational data. Moreover, in about half of the afterglows, late X-ray flares, probably due to continued activity of the central engine, are observed (O’Brien et al. 2006; Nousek et al. 2006; Zhang et al. 2006).

The light curve of GRB 050410, starting from about 2000 s from the trigger, shows a constant decay slope that can be interpreted as the third branch of the canonical light curve. The synchrotron radiation theory applied to the fireball model predicts that the temporal decay index, $\alpha$, of a GRB afterglow and the spectral slope, $\beta$, are linked by relations that depend (i) on the density profile of the external medium (Meszaros & Rees 1997; Chevalier & Li 1999); (ii) on the observer’s perception of the geometry of the expansion: spherical whenever the expansion velocity corresponds to a Lorentz factor, $\Gamma_e$, such that $\theta_h > \Gamma_e^{-1}$, and beamed for $\theta_h < \Gamma_e^{-1}$, with $\theta_h$ being the half opening angle of the jet (Sari et al. 1999; Rhoads 1999); (iii) on the observational frequency and its relation to the typical synchrotron
frequency of newly shocked electrons, $v_{\text{esc}}$, and to the cooling frequency $v_{\text{c}}$ corresponding to a synchrotron cooling time equal to the hydrodynamical expansion time (Sari et al. 1998). In particular, for fireball expansion in a uniform interstellar medium we are usually in the $v_{\text{esc}} > v_{\text{c}}$ regime and expect $\alpha = (3p - 2)/4$ and $\beta = p/2$, with the energy distribution of the electrons, $p$, greater than 2, before the jet edge effect is manifested. This relation is satisfied by GRB 050410 with a value $p = 2.08 \pm 0.05$. This value is lower than $p$ values predicted by numerical simulations (2.2–2.5), but still consistent for particle acceleration at ultraluminous shocks. From this result, we can derive a lower limit of 10 d to the time after the trigger of any jet break. The XRT light curve of GRB 050410 is therefore consistent with a pre-Swift X-ray afterglow light curve, or with the third branch of the canonical Swift afterglow light curve. The late start of XRT observations (∼2000 s after the trigger) might have prevented the detection of the previous branches.

According to the typical Swift afterglow behaviour, the early break in the X-ray light curve of GRB 050412 may be interpreted as the flat to steep transition corresponding to the end of the refreshing of the forward shock. However the measured spectral index $\beta_e = 0.3 \pm 0.2$ would imply a flat electron energy distribution with $p = 0.7 \pm 0.3$. The expected temporal slope, either for spherical expansion in a uniform medium or for a standard isotropic wind model in the $p < 2$ and $v_{\text{esc}} > v_{\text{c}}$ regime, is inconsistent with $\alpha_2$.

The values of $\alpha_1 (0.7 \pm 0.4)$, $\alpha_2 (2.8^{+0.5}_{-0.3})$ and $\beta_e (0.3 \pm 0.2)$ of GRB 050412 fit the closure relations corresponding to a jet break occurring in the $v_{\text{esc}} < v_{\text{c}} < v_{\text{c}}$ regime for $p = (2\beta_e + 1) = 1.7 \pm 0.3$ with $\alpha_1 = 3/(2\beta_e + 3)/16$ and $\alpha_2 = (2\beta_e + 7)/4$ according to Dai & Cheng (2001). An early achromatic break has also been detected in the X-rays and optical light curve for GRB 050801 (Rykoff et al. 2006; Covino et al. 2006), while achromatic breaks usually occur at $T > 10^4$ s (Blustin et al. 2006; Romano et al. 2006; Soderberg et al. 2006; Bloom et al. 2003; Frail et al. 2001; Covino et al. 2006). However, in the case of GRB 050412, this explanation is very unlikely because such an early time for the temporal break would require a very small value for the jet angle ($\theta_j < 1$ deg) which is at variance with the beaming angle ($\theta_j > 3$ deg) computed, assuming a peak energy greater than 150 keV, from the Amati (2006) and Ghirlanda et al. (2004) relations, that holds for most of the bursts.

Alternatively, the first part of the XRT light curve can be considered as the last peak of the prompt emission, and the decay rate beyond 250 s can be interpreted as due to curvature effect after an instantaneous turn off of the source (Kumar & Paniarescu 2000). Within this model the relation that should be satisfied is $\alpha_2 = 2(\beta_e + 1)$ which is in agreement with our results. After the final detection at 1 ks, the X-ray light curve may start following a typical afterglow decay without violating the later upper limits, however a drop of more than three order of magnitudes in flux within the first $10^4$ s from the trigger and before the emergence of the afterglow is uncommon to Swift GRBs. It is then possible that GRB 050412 was a burst without afterglow (a naked burst) as GRB 050421 (Godet et al. 2006).

### 4.2. Darkness

GRB 050410 and GRB 050412 do not have identified optical/infrared afterglows, therefore, it is worth considering how dark these bursts are. Both bursts are located in regions with moderate or small Galactic extinction ($E_{B-V} = 0.11$ and 0.02 for GRB 050410 and GRB 050412, respectively). The available optical upper limits for GRB 050410 are too shallow for any meaningful claim, as shown in Fig. 5 where the broad band spectral energy distribution at the time of the Misra et al. (2005) optical measurement is plotted. The comparison with the X-ray flux ($\beta_{ox} \sim 0.8$ computed at 11 h from the burst) indicates that it was a rather regular burst regards to its gamma-ray to X-ray ratio (see also Roming et al. 2006). However, the 2–10 keV flux computed at 1 h ($2.4 \times 10^{-12}$ erg cm$^{-2}$ s$^{-1}$) and at 11 h ($1.9 \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$) shows that this burst has a relatively faint X-ray afterglow (see Fig. 4 in Roming et al. 2006).

A possible interpretation of a low afterglow flux level is a low density medium (Groot et al. 1998; Frail et al. 1999; Taylor et al. 2000). Assuming that the low X-ray flux is due to a low-density circumburst medium, we derived an estimate of the interstellar medium near the GRB under some reasonable assumptions. From the detected peak energy, $E_p$, in the BAT spectrum, and using the Amati relation (Amati 2006) the values of the energy of the afterglow $E_a (=2 \times 10^{51}$ erg) and of the redshift $z (-0.4)$ were inferred. Assuming an electron index of $p = 2.5$, taking into account the decay of the afterglow and assuming that the observing frequency is between the peak frequency $v_{\text{m}}$ and the cooling frequency $v_{\text{c}}$, we derived $n < 0.01$ cm$^{-3}$. The estimate of $n$, subject to the uncertainty on $E_a$ and $p$ (which increases with $z$ and decreases with $E_a$ and $p$) is lower than the typical value of GRBs with optical afterglow ($\sim 1$ cm$^{-3}$), but similar to values which have already been derived for other GRBs (Paniarescu & Kumar 2002).

Things are considerably different in the case of GRB 050412: about 2.3 h after the burst the optical afterglow was not detected with an upper limit of $R_\gamma = 24.9$ (Kosugi et al. 2005). In the Rol et al. (2005) Fig. 2 the GRB 050412 representative point would immediately classify it as a very dark burst. However, while any possible optical afterglow for this event is undoubtedly faint already at about 2 h after the high energy event, to discuss the darkness of the burst a comparison with the detected X-ray flux is mandatory. The X-ray light curve of GRB 050412 shows a break at about 4 min after the burst and then a steep decay with a temporal index of about 2.8 (see Sect. 3.2). In computing the optical-to-X-ray spectral index at 11 h after the burst, we may either assume that the optical upper limit went on fading with $T^{-1}$ (as assumed in Jakobsson et al. 2004), or that the optical decay follows the X-ray light curve. In a similar way, the X-ray density flux computed at 11 h
from the burst can be evaluated from the extrapolation of the decay curve, or assuming that, at that time, the burst flux reached the level of the Chandra upper limit. The resulting optical-to-X-ray spectral index $\beta_{ox}$ would not clearly identify this event as dark because it ranges from −0.5 to −1 depending on how the optical and X-ray flux extrapolation are performed. Of course, the brighter the extrapolated X-ray flux, the more convincing is the classification of GRB 050412 as a dark event.

Figure 6 presents the optical upper limit by Kosugi et al. (2005) at 2.3 h from the trigger together with the X-ray spectrum computed extrapolating the XRT flux with the measured decay rate ($\alpha_b = 2.8$) and assuming no spectral variation with time (see label $a$). In the same figure, the X-ray spectrum is also computed assuming that the flux at 2.3 h was as high as the upper limit measured by XRT at 7 ks from the burst (see label $b$) and that the light curve became flat at the level of the Chandra upper limit (see label $c$; Berger & Fox 2005). However, we have seen in Sect. 4.1 that the most likely interpretation of the XRT light curve of GRB 050412 is not an afterglow, but the tail of the prompt emission from curvature effect. If this is the case, the possible underlying X-ray afterglow at 2.3 h is expected to be softer than the measured spectrum (with a photon index $\Gamma \sim 2$). This would make the X-ray spectra in Fig. 6 steeper, bringing the expected optical emission well above the observed upper limit, but it would not lead to a firm conclusion about the darkness of GRB 050412.

As last point, looking at Fig. 3 in Roming et al. (2006) both GRB 050410 and GRB 050412 appear fairly normal considering the X-ray flux at 1 h compared to their prompt y-ray flux.

5. Conclusion
We have presented a detailed analysis of the prompt and afterglow emission of GRB 050410 and GRB 050412 detected by Swift. For either burst no optical counterparts were detected. Results of the analysis can be summarised as follow:

- The prompt emission lasted $44 \pm 1$ s with a $15-150$ keV fluence of $6.3 \pm 0.3 \times 10^{-7}$ erg cm$^{-2}$ for the first burst (GRB 050410) and $27 \pm 1$ s with a $15-150$ keV fluence of $6.3 \pm 0.3 \times 10^{-7}$ erg cm$^{-2}$ for the second burst (GRB 050412). The $15-150$ keV average energy distribution of the GRB 050410 emission was fitted by a Band model with the peak energy at $53 \pm 24$ keV and a low energy slope of $-0.79 \pm 0.09$ after fixing the high energy slope to $-3$. The GRB 050412 $15-150$ keV emission was modelled with a hard ($\Gamma = 0.7 \pm 0.2$) power law suggesting a peak energy above BAT energy range.
- The GRB 050410 XRT light curve can be modelled with a single power law with a slope of $\alpha = 1.06 \pm 0.04$. The average spectrum is reproduced by an absorbed power law with a spectral index $\Gamma_x = 2.4 \pm 0.4$ and low energy absorption $N_H = 4^{+3}_{-2} \times 10^{21}$ cm$^{-2}$ which is higher than the galactic value.
- The GRB 050412 XRT light curve follows a broken power law with the first slope $\alpha_1 = 0.7 \pm 0.4$, the break time $T_{break} = 254^{+79}_{-20}$ s and the second slope $\alpha_2 = 2.8^{+0.5}_{-0.8}$. The average spectrum was fitted by a power law with a spectral index $\Gamma_x = 1.3 \pm 0.2$ and absorbed at low energies by a column consistent with the Galactic ($N_H = 2.21 \times 10^{20}$ cm$^{-2}$).
- The GRB 050410 afterglow light curve manifests the expected characteristics of the third component of the canonical Swift light curve and can be interpreted as that X-ray afterglow of a spherical fireball expanding in a uniform medium. In contrast, a rather complex phenomenology was detected in the GRB 050412 X-ray light curve because of a very early break ($\sim 250$ s). A possible explanation for the observed phenomenology suggests the detection of a tail of the prompt emission.
- Upper limits exist for the afterglows of both bursts in the optical, and the upper limit is quite severe in the case of GRB 050412. However, neither burst can be clearly classified as a dark burst according to the definition given by Jakobsson et al. (2004). GRB 050410 has a $\beta_{ox} = 0.8$ and the suppression of the optical afterglow could be attributed to a low density of the interstellar medium surrounding the burst. For the second burst, the proper evaluation of the $\beta_{ox}$ is quite difficult due to the ambiguity in the extrapolation of the X-ray light curve.

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