Accessing the population of high redshift Gamma Ray Bursts

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ABSTRACT

Gamma Ray Bursts (GRBs) are a powerful probe of the high redshift Universe. We present a tool to estimate the detection rate of high–\(z\) GRBs by a generic detector with defined energy band and sensitivity. We base this on a population model that reproduces the observed properties of GRBs detected by \textit{Swift}, \textit{Fermi} and \textit{CGRO} in the hard X–ray and \(\gamma–ray\) bands. We provide the expected cumulative distributions of the flux and fluence of simulated GRBs in different energy bands. We show that scintillator detectors, operating at relatively high energies (e.g. tens of keV to the MeV), can detect only the most luminous GRBs at high redshifts due to the link between the peak spectral energy and the luminosity (\(E_{\text{peak}} - L_{\text{iso}}\)) of GRBs. We show that the best strategy for catching the largest number of high–\(z\) bursts is to go softer (e.g. in the soft \(X\)-ray band) but with a very high sensitivity. For instance, an imaging soft \(X\)-ray detector operating in the 0.2–5 keV energy band reaching a sensitivity, corresponding to a fluence, of \(\sim 10^{-8}\) erg cm\(^{-2}\) is expected to detect \(\approx 40\) GRBs yr\(^{-1}\) sr\(^{-1}\) at \(z \geq 5\) (\(\approx 3\) GRBs yr\(^{-1}\) sr\(^{-1}\) at \(z \geq 10\)). Once high–\(z\) GRBs are detected the principal issue is to secure their redshift. To this aim we estimate their NIR afterglow flux at relatively early times and evaluate the effectiveness of following them up and construct usable samples of events with any forthcoming GRB mission dedicated to explore the high–\(z\) Universe.

Key words: Gamma-ray: bursts — Cosmology: observations, dark ages, re–ionization, first stars

1 INTRODUCTION

The study of the Universe before and during the epoch of reionization represents one of the major themes for the next generation of space and ground–based observational facilities. Many questions about the first phases of structure formation in the early Universe are still open: When and how did first stars/galaxies form? What are their properties? When and how fast was the Universe enriched with metals? How did reionization proceed?

Thanks to their brightness, Gamma Ray Bursts (GRBs) can be detected up to very high redshift, as already shown by the detection of GRB 090423 at \(z = 8.2\) (Salvaterra et al. 2009; Tanvir et al. 2009) and GRB 090429 at \(z \sim 9.4\) (Cucchiara et al. 2011). Thus, GRBs represent a complementary, and to some extent unique, tool to study the early Universe (see e.g. McQuinn et al. 2009; Amati et al. 2013). A statistical sample of high–\(z\) GRBs can provide fundamental information about: the number density and properties of low-mass galaxies (Tanvir et al. 2012; Basa et al. 2012; Salvaterra et al. 2013; Berger et al. 2014); the neutral–hydrogen fraction (Gallerani et al. 2008; Nagamine et al. 2008; McQuinn et al. 2008; Robertson & Ellis 2012); the escape fraction of UV photons from high–\(z\) galaxies (Chen et al. 2007; Fynbo et al. 2009); the early cosmic magnetic fields (Takahashi et al. 2011), and the level of the local inter–galactic radiation field (Inoue et al. 2010).
Moreover, GRBs will also allow us to measure independently the cosmic star–formation rate, even above the limits of current and future galaxy surveys (Ishida et al. 2011), provided that we are able to quantify the possible biases present in the observed GRB redshift distribution (Salvaterra et al. 2012; Trenti et al. 2013; Vergani et al. 2014). Even the detection of a single GRB at $z > 10$ would be extremely useful to constrain dark matter models (de Souza et al. 2013) and primordial non–Gaussianities (Maio et al. 2012). Finally, it has been argued that the first, metal–free stars (the so–called PopIII stars) can result in powerful GRBs (Meszaros & Rees 2010; Komisarov & Barkov 2010; Suwa & Yoka 2011; Piro et al. 2014). Thus GRBs offer a powerful route to directly identify such elusive objects and study the galaxies in which they are hosted (Campisi et al. 2011). Even indirectly, the role of PopIII stars in enriching the first galaxies with metals can be studied by looking to the absorption features of PopII GRBs blowing out in a medium enriched by the first PopIII supernovae (Wang et al. 2012; Ma et al. 2014 in prep).

Specific predictions on the detection rate of high–$z$ GRBs (Bromm & Loeb 2002; Gorosabel et al. 2004; Daigne, Rossi & Mochkovitch 2006; Salvaterra & Chincarini 2007; Salvaterra et al. 2008; Butler et al. 2010; Qin et al. 2010; Salvaterra et al. 2012; Littlejohns et al. 2013) are of fundamental importance for the design of future missions. In particular, it is often believed that the population of high redshift GRBs could be easily accessed with soft X–ray instruments, due to the $(1 + z)^{-1}$ cosmological redshift of their characteristic peak spectral energy. However, the peak energy is strongly correlated with the burst luminosity/energy (Yonetoku et al. 2004; Amati et al. 2002) and, therefore, the trigger energy band and the detector sensitivity are strongly interlaced.

The typical prompt emission peak energy $E_{\text{peak}}$ of GRBs detected by past/present instruments extends from a few keV up to a few MeV. The distribution of the observer frame peak energy versus redshift of the 185 GRBs with measured spectral parameters and redshift $z$ (up to September 2014) is shown in Fig. 1 (see also Gruber et al. 2011). The spectroscopically confirmed highest redshift GRB 090423 ($z = 8.2$) has an observer frame $E_{\text{peak,obs}} \sim 90$ keV (von Klienein et al. 2009) as measured by Fermi–GBM. Fig. 1 shows the absence of GRBs with low measured $E_{\text{peak,obs}}$ at high redshifts. This is a consequence of the spectral–luminosity correlation $E_{\text{peak}} - L_{\text{iso}}$ (where $L_{\text{iso}}$ is the isotropic equivalent peak luminosity – Yonetoku et al. 2004) and the limited sensitivity of current GRB detectors. In other words, we can access, at high redshifts, only to the most luminous GRBs that have the highest $E_{\text{peak}}$. This compensates the $(1 + z)^{-1}$ decrease of $E_{\text{peak}}$ expected if $E_{\text{peak}}$ were independent of luminosity.

This paper aims to study how these two instrumental properties can be optimized for detecting the largest number of high redshift bursts. We base that on a population synthesis code (§2) anchored to the observed properties (prompt emission flux and fluence and optical afterglow flux) of the GRBs detected by Swift, Fermi, BATSE (§3). In §4 we provide a general tool (§4) that allows to predict the detection rate of GRBs for a detector with specified energy band and sensitivity. Beside their detection, we also study the possibility to follow up the high–$z$ GRB population in the X–ray and NIR bands through the characterization of their afterglow flux level (§5). A standard cosmology with $h = \Omega_{\Lambda} = 0.7$ and $\Omega_M = 0.3$ is assumed.

![Figure 1. Observer frame peak energy of the $\nu F_\nu$ spectrum versus redshift of 185 GRBs with measured redshift $z$ and well determined prompt emission $E_{\text{peak}}$. Different symbols (as displayed in the legend) correspond to detectors/instruments that provided the measure of $E_{\text{peak}}$.](image-url)
function rather than the GRB formation efficiency. We have tested also this assumption and show in §5 that our conclusions are unchanged.

(3) To compute the flux and fluence of GRBs in a given energy range, we need to associate a spectrum to each simulated burst. Assuming that all bursts have a spectrum described by a double power law function smoothed at the peak energy $E_{\text{peak}}$, we assign to each simulated burst a low energy photon spectral index $\alpha$ and a high energy photon spectral index $\beta$ drawn from Gaussian distributions centered at $-1$ and $-2.3$ with $\sigma = 0.2$, respectively (e.g. Kaneko et al. 2006; Nava et al. 2011; Goldstein et al. 2012).

(4) The spectral peak energy $E_{\text{peak}}$ is obtained through the $E_{\text{peak}} - L_{\text{iso}}$ correlation (Yonetoku et al. 2004). $L_{\text{iso}}$ represents the peak isotropic luminosity, i.e. related to the flux at the peak of the $\gamma$-ray light curve. We adopt the $E_{\text{peak}} - L_{\text{iso}}$ correlation obtained with the complete BAT6 sample (Nava et al. 2012): $\log{(E_{\text{peak}})} = 29.6 + 6.61 \log{(L_{\text{iso}})}$. We account for the scatter $\sigma = 0.29$ dex of the data points around this correlation (Nava et al. 2012).

(5) Similarly, in order to have also a fluence associated to each simulated burst, we adopt the $E_{\text{peak}} - E_{\text{iso}}$ correlation (Amati et al. 2002) between the peak energy and the isotropic equivalent energy $E_{\text{iso}}$, as derived with the BAT6 sample (Nava et al. 2012): $\log{(E_{\text{peak}})} = 29.6 + 0.61 \log{(E_{\text{iso}})}$. This correlation is used to derive $E_{\text{iso}}$ and $L_{\text{iso}}$.

Note that our simulation approach does not need to specify the distribution of $E_{\text{peak}}$ from where assign the values of this parameter to the simulated bursts. Indeed, the starting assumption of the simulation is the luminosity function. Therefore, the simulated GRB population will have a distribution of $L_{\text{iso}}$ which is the form of the assumed luminosity function. It is assumed $E_{\text{peak}} - L_{\text{iso}}$ correlation which transforms the $L_{\text{iso}}$ distribution into the distribution of $E_{\text{peak}}$.

The latter passage is not a 1:1 mapping since we allow for the scatter of the correlations. For both the $E_{\text{peak}} - E_{\text{iso}}$ and the $E_{\text{peak}} - L_{\text{iso}}$ correlation the scatter that we adopt represents the $\sigma$ of the gaussian distribution of the distance of the data points measured perpendicular to the best fit line of the correlations. It is still debated if and how much these correlations are affected by selection effects (Band & Preece 2005; Nakar & Piran 2005; Butler et al. 2007; Butler, Koczi & Bloom 2009; Shahmoradi & Nemiroff 2011; Kocevski 2012) despite some tests suggest that this might not be the case (Bosnjak et al. 2008; Ghirlanda et al. 2008; Nava et al. 2008; Amati, Frontera & Guidorzi 2009; Grimm et al. 2009; Ghirlanda et al. 2012; Dainotti et al. 2014; Mochkovitch & Nava 2014). However, there seems to be an agreement that, if not properly a correlation, there could be a boundary in the $E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - L_{\text{iso}}$ plane which divides the plane in two regions: the right hand side of the correlations lacking of bursts with large $E_{\text{iso}}$ and $L_{\text{iso}}$ (whose lack might be due to some physical reason - e.g. Nakar & Piran 2005) and the left hand side of the correlations (corresponding to GRBs with low $E_{\text{iso}}$ and $L_{\text{iso}}$) which might be affected by instrumental biases. If so, the plane could be uniformly filled with bursts on the left hand side of the correlations (i.e. at intermediate/low $E_{\text{iso}}$, $L_{\text{iso}}$) with no correlation between $E_{\text{iso}}$ and $E_{\text{peak}}$ and $L_{\text{iso}}$ and $E_{\text{peak}}$. A fraction of these events could be missed due to some instrumental selection effects that shapes its cut in the plane so to make an apparent correlation. We have tested also this hypothesis and discuss it in §5.

With these assumptions we derive the 1-s peak flux $P$ of each simulated burst in a given energy range $\Delta E = [E_1, E_2]$:

$$P_{\Delta E} = \frac{L_{\text{iso}}^{E_1^2}}{4\pi d_L(z)^2} \cdot \frac{\int_{10^5 \text{keV}/(1+z)}^{10^4 \text{keV}/(1+z)} E N(E) dE}{\int_{10^4 \text{keV}/(1+z)}^{10^5 \text{keV}/(1+z)} E N(E) dE}$$

where $N(E)$ is the observer frame photon spectrum and $d_L(z)$ is the luminosity distance corresponding to the redshift $z$. The fluence $F$ is:

$$F_{\Delta E} = \frac{E_{\text{iso}}(1+z)}{4\pi d_L(z)^2} \cdot \frac{\int_{10^5 \text{keV}/(1+z)}^{10^4 \text{keV}/(1+z)} E N(E) dE}{\int_{10^4 \text{keV}/(1+z)}^{10^5 \text{keV}/(1+z)} E N(E) dE}$$

The integrals at the denominators are performed over the rest frame 1keV–10MeV energy range, which is typically adopted to derive $E_{\text{iso}}$ and $L_{\text{iso}}$.

3 SIMULATION NORMALIZATION AND CONSISTENCY CHECKS

The simulated population of GRBs is normalized to the actual population of bright bursts detected by Swift/BAT. The BAT6 sample of 512 considered GRBs detected by Swift/BAT with peak flux $P \geq 2.6$ ph cm$^{-2}$ s$^{-1}$ (integrated in the 15–150 keV energy range) selected only for their favorable observing conditions (Jakobsson et al. 2006). The sample contains 58 GRBs and is 95% complete in redshift.

We have extracted from the current Swift sample (773 events detected until July 2014 with $T_{\text{iso}} \geq 2$ s) the 204 GRBs with 1-s peak flux $P \geq 2.6$ ph cm$^{-2}$ s$^{-1}$ (i.e. the same flux threshold used to define the BAT6). Considering a typical field of view of 1.4 sr and a mission lifetime of approximately 9.5 years, we estimate a detection rate by Swift of $\sim 15$ events yr$^{-1}$ sr$^{-1}$ with peak flux $P \geq 2.6$ ph cm$^{-2}$ s$^{-1}$. We normalize the simulated GRB population to this rate.

The peak flux cumulative rate distribution of the real Swift sample of 204 GRBs with $P \geq 2.6$ ph cm$^{-2}$ s$^{-1}$ is shown in the top panel of Fig. 2 (green hatched region representing the statistical uncertainty on the rate). Swift has detected many more GRBs with peak flux smaller than this limit which is about six times larger than the actual Swift flux limit. The consistency of the simulated population with the entire Swift sample is discussed in §4.1. The corresponding distribution of the simulated GRB population is represented by the cyan solid line in Fig. 2. As shown in the bottom left panel of Fig. 2, the simulated bursts with $P_{15–150} \geq 2.6$ ph cm$^{-2}$ s$^{-1}$ (cyan solid line) have a redshift distribution consistent with that of the real BAT6 sample (hatched histogram).

Note that the comparison of the population of simulated bursts with the real Swift GRB sample shown in Fig. 2 (top panels and bottom left panel) are consistency checks. Indeed, their scope is to show that the assumptions (§2), on which the code is based, are correctly implemented and reproduce the population of bursts (i.e. Swift bright events) from which they are derived.

3.1 The Fermi GBM and BATSE samples

An interesting test is to verify if the simulated GRB population is representative also of larger samples of GRBs detected by other instruments besides Swift–BAT.

http://swift.gsfc.nasa.gov/docs/swift/archive/gra_table/
The Gamma Burst Monitor (GBM) on board Fermi has detected many bursts and systematic analysis of their spectral properties exist (Nava et al. 2011; Goldstein et al. 2012; Gruber et al. 2014). The first two years GBM sample (Goldstein et al. 2012) contains 478 GRBs with the corresponding spectral parameters, peak flux $P$ and fluence $F$. We considered the flux integrated in the 50–300 keV energy range and cut the GBM sample at $P \geq 0.7$ ph cm$^{-2}$ s$^{-1}$ in order to overcome the possible incompleteness of the sample at lower fluxes, obtaining 293 GBM bursts. The GBM is an all sky monitor that observes on average $\sim 70\%$ of the sky. Therefore, the average GBM detection rate of bursts, with $P \geq 0.7$ ph cm$^{-2}$ s$^{-1}$, is 17 events yr$^{-1}$ sr$^{-1}$. Fig. 2 (top left panel) shows that the 50–300 keV flux distribution of real GBM bursts (hatched orange region) is consistent with that of the simulated population (blue solid line).

We have considered also the BATSE 4B catalog (Meegan et al. 1998) containing 1496 bursts with estimated peak flux $P$ and fluence $F$ (both integrated in the 50–300 keV energy range). Also in this case we cut the sample to $P \geq 0.7$ ph cm$^{-2}$ s$^{-1}$ (i.e. the same level of the GBM), to overcome for incompleteness at low fluxes, and obtain 964 events. Considering an average $\sim 75\%$ portion of the sky observed by BATSE, the detection rate is $\sim 22$ events yr$^{-1}$ sr$^{-1}$ above the considered flux limit. The BATSE peak flux distribution (shaded grey region in Fig. 2) is consistent with the simulation (blue solid line in the same figure).

The top right panel of Fig. 2 shows the cumulative fluence distributions of the Swift, BATSE and GBM samples as shaded regions (representing the $1\sigma$ statistical uncertainties). The peak flux and fluence distributions of GBM and BATSE are similar (see Nava et al. 2011a)$^2$. The solid lines in the top right panel of Fig. 2 represent the simulated GRB population.

### 3.2 The afterglow

The study of high redshift GRBs relies on the capabilities of securing a redshift for these events. This depends on the brightness of

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$^2$ The three catalogs contain some bursts with only their peak flux or only their fluence reported. This is the reason why the cumulative peak flux and fluence distributions saturate at slightly different levels for the same instrument.
their afterglow in the NIR band. In order to study and predict the afterglow flux of the simulated GRB population, we implemented in the code the afterglow emission model as developed in van Eerten (2010, 2011). This corresponds to the afterglow emission from the forward shock of a decelerating fireball in a constant interstellar density medium. We assume a constant efficiency $\eta = 0.2$ of conversion of kinetic energy to radiation during the prompt phase and a typical jet opening angle of $7^\circ$ (corresponding to the mean value of the reconstructed distribution of $\theta_{jet}$ – Ghirlanda et al. 2013). For the ISM density we assume a Gaussian distribution centered at $n = 3$ cm$^{-3}$ and extending from 1 to 30 cm$^{-3}$.

We use the afterglow $R$ flux distribution of the BAT6 sample (Melandri et al. 2014 – corrected for extinction, see also Covino et al. 2013) to fix the parameters of the external shock micro-physics (e.g. Sironi, Spitkovsky & Arons 2013): the fraction of energy that the external shock shares with electrons and magnetic field, $\epsilon_e$ and $\epsilon_B$ and the slope of the shock accelerated electrons $p$. Assuming $\epsilon_e = 0.02$, $\epsilon_B = 0.008$ and $p = 2.3$ (which also reproduce the radio afterglow flux of the BAT6 sample - Ghirlanda et al. 2013b) we show that the $R$ flux (computed at 11h) distribution of the simulated bright bursts (i.e. with $P > 2.6$ ph cm$^{-2}$ s$^{-1}$ – cyan solid line in the bottom right panel of Fig. 2) is consistent with that of the BAT6 sample (hatched green histogram). A Kolmogorov–Smirnov test results in a probability of 0.05 that the two distributions are drawn from the same parent population. Differently from the other panels, the aim of the bottom right panel of Fig.2 is that of fixing the free afterglow parameters of the simulated GRB population in order to match the observed flux distribution of the BAT6 sample of GRBs (solid filled histogram). We do not pretend to explore the afterglow parameter space here (which would require detailed modelling of individual bursts - e.g. Zhang et al. 2014) but rather fix the parameters (assumed equal for all simulated bursts) in order to predict the typical afterglow flux of the simulated burst population. Therefore, we consider the agreement of the simulated (solid line) and real GRB population afterglow flux distribution shown in the bottom panel of Fig.2 satisfactory. With these parameters we can predict the afterglow emission of the simulated GRB population at any time and any frequency.

4 RESULTS

GRBs are detected by current instruments as a significant increase of the count rate with respect to the average background. This is the rate trigger and it is typically implemented by measuring the count rate on several timescales and different energy bands (e.g. Lien et al. 2014 for Swift–BAT). Swift–BAT also adopts the image

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**Figure 3.** Cumulative peak flux distributions representing the rate, i.e. the number of GRBs yr$^{-1}$ sr$^{-2}$, with peak flux $\geq P$. Different energy ranges where the peak flux $P$ is computed are shown with different colors (as shown in the legend). The typical uncertainty on the predicted rates (for any energy range) is shown by the vertical bar (see §5). Top panel: entire population of simulated GRBs. Bottom panel: population of high redshift GRBs: $z \geq 5(10)$ shown by the solid (dotted) line. For the soft energy band 0.2–5 keV (shown by the red line) a typical $N_H = 2 \times 10^{21}$ cm$^{-2}$ has been assumed to account for the absorption.
trigger mode: this searches for any new source in images acquired with different integration times. In general both triggers are satisfied by most GRBs but the image trigger is particularly sensitive to dim/long GRBs: in the Swift GRB sample the relatively small fraction of bursts with only image triggers have a smaller peak flux than the rest of the bursts (Toma et al. 2011). The time dilation effect at particularly high redshifts makes GRB pulses appear longer. Therefore, image trigger can better detect high–z events.

The rate trigger is particularly sensitive to the “spikiness” of GRBs and, therefore, to the peak flux $P$, while the image trigger is sensitive to the time integrated flux of the burst, i.e. its fluence. For these reasons, we present here the peak flux $P$ and fluence $F$ distributions of the simulated GRB population.

Both $P$ and $F$ can be computed on a specific energy range $\Delta E$ in our code (Eq. 4, 5). To present our results, based on the past/present GRB detectors which were mainly either collimated scintillators or imaging coded masks, we have considered the 50–300 keV energy range where both BATSE and GBM operate (representative of scintillator detectors) and the 15–150 keV energy range of Swift–BAT (representative of coded masks). For the predictions of the detection of high–z GRBs we considered, for reference, the soft energy range 2–50 keV (the BeppoSAX Wide Field Cameras - Jager et al. 1997 - were actually operated in the 2–20 keV energy range and similarly the Wide X-ray Monitor - Kawai et al. 1999 - on board Hete–II), where a coded mask instrument could operate and the very soft range 0.2–5 keV, appropriate for an instrument like Lobster (Osborne et al. 2013).

### 4.1 Peak flux and Fluence

We have computed the peak flux in the four energy bands given above for the entire population of simulated GRBs. The cumulative peak flux distributions are shown in Fig. 3. We show the rate of GRB in units of yr$^{-1}$ sr$^{-1}$. The total rate (where the curves saturates at low fluxes) is $\sim$ 1600 GRBs yr$^{-1}$ sr$^{-1}$. The flux where the curves saturates depends on the energy range where $P$ is computed. The curve showing the flux in the 0.2–5 keV band (red line) is slightly different with respect to the other bands. Indeed, to account for the absorption in the soft X–ray band, we have applied a systematic correction of the flux by a factor 1.32, which corresponds to the ratio between the intrinsic and absorbed flux for a typical power law photon spectrum ($N(E) \propto E^{-\Gamma}$) with photon index $\Gamma = 1$ and assuming an average $N_H = 2 \times 10^{21}$ cm$^{-2}$ at $z = 0$ (Evans et al. 2009; Willingale et al. 2013).
population of GRBs at $z \geq 5$ (solid lines) and at $z \geq 10$ (dotted lines).

The curves in Fig. 3 can be used to predict the detection rate of an instrument operating in any of the four energy bands considered once its flux limit is known. A note on the use of Fig. 3: since fluxes in different energy ranges are represented, the threshold (i.e. sensitivity limit of a given instrument) should be applied to the corresponding curve.

For instance, assuming that the flux limit of Swift–BAT is $\sim 0.4$ ph cm$^{-2}$ s$^{-1}$ in the 15–150 keV energy range, the top panel of Fig. 3 shows that (cyan line) this limit corresponds to $\sim 56$ GRBs yr$^{-1}$ sr$^{-1}$. Considering an average field of view of 1.4 sr and a 9.5 yr mission lifetime, this rate corresponds to 745 GRBs detected by Swift with $P \geq 0.4$ ph cm$^{-2}$ s$^{-1}$ (computed in the 15–150 keV energy band). This is in agreement with the $\sim 730$ real GRBs (with $T_{90} \geq 2$ s) present in the Swift on line catalog with peak flux above this limit. Similarly one can use the bottom panel of Fig. 3 to compute the rate of GRBs at high redshift that can trigger Swift. We predict that the rate of GRBs at $z \geq 5$ detectable by Swift at a level of $P \geq 0.4$ ph cm$^{-2}$ s$^{-1}$ in the 15–150 keV should be 1.2 yr$^{-1}$ sr$^{-1}$ (corresponding to $\sim 16$ GRBs over the present mission lifetime consistent with the observed number).

In the Fermi GRB population, instead, assuming a flux limit of 0.7 ph cm$^{-2}$ s$^{-1}$ in the 50–300 keV energy range and considering the corresponding (blue) curve in Fig. 3, we predict a rate of 15 yr$^{-1}$ sr$^{-1}$ over all redshifts (top panel of Fig. 2), and a rate of 0.1 yr$^{-1}$ sr$^{-1}$ at $z \geq 5$ (bottom panel of Fig. 2). These rates are consistent with the Fermi detection rate above this flux limit.

Fig. 4 shows the fluence cumulative distribution of the simulated population. Color codes are as in Fig. 3. We note that the curves corresponding to different energy ranges are very similar at relatively low fluence values. This is because we show here the energy fluence, i.e. in units of erg cm$^{-2}$ (as typically reported in GRB databases). In the appendix (Fig. A1) the same cumulative curves are shown with the photon fluence (i.e. in units of ph cm$^{-2}$) which might also be useful in estimating the detection rate of GRBs for an instrument working with image triggers. As explained for the peak flux, each curve represented in Fig. 3 should be compared with the fluence limit in the corresponding energy range.

### 4.2 High energy detector triggers

Current GRB detectors, operating at energies $\geq 10$ keV, are detecting the most luminous GRBs at high redshifts. Indeed, due to the $E_{\text{peak}} - L_{\text{iso}}$ correlation, these events have relatively high peak energies. Fig. 5 shows the observer frame peak energy of real GRBs detected by different instruments (as labeled) versus their redshift (same as Fig. 2) together with the entire simulated GRB population (grey region). At high $z$ the detection of the most luminous bursts, due to the $E_{\text{peak}} - L_{\text{iso}}$ correlation, also selects the GRBs with the largest peak energies. This effect can also be seen in Fig. 6 which shows the observer frame peak energy versus the bolometric flux for the real 185 GRBs with well constrained spectral parameters and for the simulated GRB population (same symbols of Fig. 5). Here we also highlight (yellow region) the simulated population of GRBs at $z \geq 5$. We note that, due to the $E_{\text{peak}} - L_{\text{iso}}$ correlation, a correlation is present in the observer frame between the observed peak energy and the peak flux (e.g. Nava et al. 2008). Through Fig. 6 one can understand that actual GRB detectors, most sensitive from 10 keV up to a few MeV, select those bursts with peak energy in this energy range. These events, due to the existence of the $E_{\text{peak}} - L_{\text{iso}}$ correlation, are also the brightest (and most luminous) bursts although their number is shaped by an overall decreasing luminosity function.

Fig. 6 shows that in order to efficiently detect high redshift GRBs (yellow symbols) one needs a detector working in a softer energy band (e.g. 0.1–10 keV) but also much more sensitive than current detectors.

We have considered four energy bands $\Delta E$ based on two classes of detectors: imaging coded mask detectors, typically operated up to a few hundreds of keV and scintillator detectors operating in 10 keV–1 MeV range. It is clear that the hunt for high–$z$ GRBs is optimized with detectors operated in the soft energy range, i.e. few keV. However, it is worth exploring the rate of detections of GRBs (and high–$z$ bursts) by both types of detectors. Indeed, for a configuration with both these detectors, for instance, while the detection

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure5.png}
\caption{Observer frame peak energy versus redshift. Real GRBs with measured $z$ and well constrained $E_{\text{peak}}$ (185 GRBs) are shown with different symbols (as described by the legend). The grey cloud of points represents the simulated GRB population. The dark/light grey contour represents the 68(95)% containment region of the simulated bursts. The plot is truncated at $z = 9$ for clarity.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure6.png}
\caption{Observer frame peak energy versus bolometric flux. Real GRBs with measured $z$ and well constrained prompt emission spectral peak energy (185 GRBs) are shown with different symbols. The grey cloud of points represents the simulated GRB population. Yellow points are GRBs at $z > 5$.}
\end{figure}
rate of high-z bursts is maximized by the soft energy detector, the study of the GRB prompt emission properties (spectral shape, luminosity etc.) is possible for those bursts also detected by the high energy detector.

Fig. 7 shows the 50–300 keV peak flux cumulative rate distribution of the simulated GRB population for different cuts of their 0.2–5 keV energy fluence (as labeled). We also show the rate for GRBs at $z \geq 5$ and $z \geq 10$ (blue dashed and red dotted lines, respectively). For a soft X-ray detector (working in the 0.2–5 keV energy range) with a sensitivity threshold of $10^{-7}$, $10^{-8}$, $10^{-9}$ and $10^{-12}$ erg cm$^{-2}$, these curves serve to estimate the rate of common triggers for two instruments: one working in the 0.2–5 keV energy range and one in the 50–300 keV energy range, once both have assigned fluence and peak flux thresholds, respectively.

**Figure 7.** Cumulative peak flux (in the 50–300 keV energy range) distribution for different cuts of the soft (0.2–5 keV) energy fluence (as shown for the four solid lines). The solid, dashed and dotted lines show the entire, $z \geq 5$ and $z \geq 10$ population of simulated bursts. The four lines for each set correspond to the 0.2–5 keV fluence cuts of $F \geq 10^{-7}$, $10^{-8}$, $10^{-9}$ and $10^{-12}$ erg cm$^{-2}$. These curves serve to estimate the rate of common triggers for two instruments: one working in the 0.2–5 keV energy range and one in the 50–300 keV energy range, once both have assigned fluence and peak flux thresholds, respectively.

**Figure 9.** Cumulative distributions of the (0.3–10 keV) X-ray flux at 5 h after the burst. Same symbols as in Fig. 5.

$z \geq 5(10)$ (considering a GRB detector with a limiting 0.2–5 keV fluence $\geq 10^{-8}$ erg cm$^{-2}$).

Finally we derive the X-ray (0.3–10 keV) flux of the simulated GRB population. This is interesting for the use of GRBs as probes of the chemical composition and properties of the intervening medium (e.g. Campana et al. 2011) through the metal absorption edges imprinted on their X-ray spectra.

The X-ray properties of the GRBs of the BAT6 sample have been presented in D’Avanzo et al. (2012). They found that the X-ray luminosity is correlated with both the prompt emission $\gamma$-ray isotropic luminosity and energy ($L_{\text{iso}}$ and $E_{\text{iso}}$ respectively - Amati et al. 2002; Yonetoku et al. 2004). There is evidence that the early X-ray emission observed in GRBs has a different origin to the afterglow produced at external shocks (Ghisellini et al. 2009). Besides there could be a connection between the prompt and X-ray emission (Margutti et al., 2013). In particular, the early time emission in the X-ray band could be due to an emission component related to the long lived activity of the central engine (invoked also by late time X-ray flares observed in the Swift XRT light curves – Burrows et al. 2007). Therefore, we estimated the X-ray flux of the simulated GRB population through the empirical correlations found by D’Avanzo et al. (2012). Fig. 9 shows the cumulative distribution of the flux in the 0.3–10 keV energy range for different cuts of the 0.2–5 keV fluence.

With a Target Of Opportunity (TOO) reaction time of 4-5 hours Athena (Nandra et al. 2013) will be able to provide high resolution spectroscopy for a large number of GRB afterglows. In order to enable high resolution spectroscopy in the microcalorimeter (XIFU) instrument, that delivers 2.5 eV resolution, a total fluence of $10^{50}$ $\text{cts}$ is needed (Jonker et al. 2013). This corresponds to typical afterglow flux of $\geq 10^{-12}$ erg cm$^{-2}$ s$^{-1}$ with an integration time of $\sim 50$–100 ksec. With this flux limit, the expected rate of GRBs is $3(0.2)$ yr$^{-1}$ sr$^{-1}$ at $z \geq 5(10)$.

**4.3 Afterglow**

In addition to the detection of the high redshift GRB population, it is fundamental to assess their redshifts. This is possible through early time NIR follow up observations. To this aim we have computed the NIR flux of the simulated GRB population as described in §3. Fig. 8 shows the cumulative $J$ band flux distribution for the GRBs at $z \geq 5$ (solid lines) and $z \geq 10$ (dashed lines) considering different thresholds of their 0.2–5 keV energy fluence.

A way to optimize the follow up of high redshift GRBs could be with a dedicated NIR telescope on board any GRB dedicated satellite trough rapid slewing. Assuming a 1 m telescope in space we expect H~22.5 in 500 seconds of integration and H~22 in 1h for imaging and low (R=20) resolution spectroscopy. Higher resolution spectroscopy (e.g. R=1000) , needed for metallicity studies, can be performed for afterglows brighter than H~18. With these estimates we evaluate, for imaging and assuming a rapid follow up i.e. within 500s, a rate of $\sim 40$ GRBs yr$^{-1}$ sr$^{-1}$ at $z \geq 5$ and 3 yr$^{-1}$ sr$^{-1}$ at $z \geq 10$ (with 0.2–5 keV fluence $\geq 10^{-8}$ erg cm$^{-2}$). Metallicity studies could be performed for $\sim 30(1.5)$ GRBS yr$^{-1}$ sr$^{-1}$ at $z \geq 5(10)$.
High-z GRBs

Figure 8. Cumulative NIR flux distribution of the afterglow of GRBs at $z > 5$ and $z > 10$ (blue and red lines respectively) at 500 s for different cuts on the 0.2–5 keV fluence. For $5 < z < 10$ we considered the $J$ band and for $z > 10$ the $H$ band. We assume $A_v = 0$ for the population of high redshift GRBs. The dotted lines show the $J$ flux at 1 h.

such a case the Athena observing efficiency will be close to 100% and the TOO reaction time would be also minimized. For a much larger FOV, ($> 1/2$ sky), the number of GRB follow up by Athena will, on the contrary reduce to 50%.

5 DISCUSSION

We have presented the prompt and afterglow properties of a synthetic population of long GRBs. The main assumptions of the simulations are the luminosity function and the GRB formation rate (proportional to the star formation rate). GRB prompt emission properties are derived through the empirical correlations between the peak energy of their spectra and the isotropic equivalent energy and luminosity ($E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - E_{\text{iso}}$ correlations). The simulated population is normalized to the bright sample of GRBs detected by Swift (i.e. GRBs with peak flux $P_{15-150\text{keV}} \geq 2.6 \text{ ph cm}^{-2} \text{s}^{-1}$). The simulated population also reproduces the properties (redshift distribution and $R$ afterglow flux distribution) of these real bursts. We have shown that the simulated population is representative also of the larger population of bursts detected by Fermi and BATSE.

The detection rates presented are based on the best fit values of the assumed GRB formation rate (Eq. 2) and their luminosity function (Eq. 3). The main source of uncertainty for the predictions of the rates of high redshift bursts is the strength $\delta$ of the evolution with redshift of the GRB formation rate. Considering $\delta = 1.7 \pm 0.5$ (S12), the rates can be larger/smaller by a factor $\sim 1.5$. This only affects the absolute rate of detection and not the comparison of the fraction of bursts accessible with instruments working in different energy bands as those presented here ($\S 4.2, 4.3$).

In general our results show that the largest rate of high-z GRBs can be detected with a soft X-ray detector (e.g. operated in the 0.2–5 keV energy range like a Lobster-type wide-field focussing X-ray) because this is where the bulk of the high-z GRBs have their peak energy (due to the cosmological redshift). However, such an instrument should be designed so to have a sensitivity that accounts properly for the the presence of a link between the $E_{\text{peak}}$ and the luminosity/energy of GRBs ($E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - E_{\text{iso}}$ correlations). To assess a population of GRBs say a factor of ten softer in $E_{\text{peak}}$ requires a sensitivity improvement of a factor $\sim 100$. This is due to the slope of the observer frame distribution of the points in Fig.6 which is a result of the $E_{\text{peak}} - E_{\text{iso}}$ correlation. The purpose of this work is to provide a tool for de-
signing instruments for detecting a large sample of GRBs to study the high–z Universe.

The results presented so far are based on the set of assumptions described in §2: the evolution of the GRB formation rate with redshift (Eq. 1) and the $E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - L_{\text{iso}}$ correlations which are used, considering also their scatter, to link the energetic/luminosity of the simulated bursts with their peak energy.

The first assumption is motivated by the fact that an evolution of the GRB density is also consistent with the metallicity bias as found from the study of GRB hosts (e.g. Vergani et al. 2014), and it is theoretically expected within the collapsar model. However, also the alternative scenario in which the luminosity function evolves with redshift has been shown to be consistent with the observations (e.g. Salvaterra et al. 2012). For completeness we also have explored this possibility, assuming the GRB rate without any redshift evolution (i.e. $\delta = 0$ in Eq.1) but, instead, a luminosity function described by a power law with a break luminosity $L_{\text{cut}} \propto (1 + z)^{2.1}$. This model increases the fraction of luminous bursts at high redshifts: the results are shown in Fig.12 by the dashed lines. Compared with the results obtained with an evolving GRB rate (§2 - shown by the solid lines in Fig.12), the global effect is to reduce the rate of dim bursts due to the increase of the high redshift and bright bursts (bottom panel of Fig.12). However, these differences are consistent with the typical uncertainty on the estimated rates (shown by the vertical bar in Fig.12).

The other assumptions, i.e. the $E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - L_{\text{iso}}$ correlations can also be tested. We have assumed (§2) these two correlations with their scatter. However, it is still debated if they are due to instrumental selection effects which, if present, should limit the detection of GRBs of intermediate/lower luminosity/energy, i.e. those on the left hand side of these correlations (in the $E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - L_{\text{iso}}$ correlations we typically plot the x–axis representing the isotropic energy $E_{\text{iso}}$ or luminosity $L_{\text{iso}}$), Although excluded by recent simulations (Ghirlanda et al. 2012) we have considered the extreme case of a uniform distribution of simulated bursts on the left hand side of the $E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - L_{\text{iso}}$ correlations. In practice we assume that the $E_{\text{peak}} - E_{\text{iso}}$ and $E_{\text{peak}} - L_{\text{iso}}$ correlations are boundaries in their respective planes (e.g. Nakar & Piran 2005; Butler Bloom & Poznanski 2010) which are therefore divided in two regions: on the right hand side of the correlations there are no bursts (if they were present we should have detected) while on the left hand side there is no intrinsic correlation between e.g. $E_{\text{peak}}$ and $L_{\text{iso}}$($E_{\text{iso}}$). The results obtained with this assumption are shown by the dashed lines in Fig.13. From the comparison with the results (solid lines) obtained with the set of assumptions of §2 (i.e. assuming instead the correlations with their scatter), it appears that the difference is minimal and consistent within the uncertainty on the estimated rates.

6 CONCLUSION

Through our code we can derive the prompt emission flux and fluence and the afterglow flux (at any time and frequency) of the population of GRBs distributed up to $z = 20$. We note that our code does not include the possibility that the GRB rate at high redshift is enhanced by the primordial massive (popIII) stars which could even be dominating at $z \geq 10$ (Campisi et al. 2011). We have derived for the first time also the afterglow $J$ and $H$ band flux for high redshift GRBs. This is important because it can be used to assess the fraction of detected GRBs whose afterglow can be observed (or spectrum acquired) with an IR telescope (in order to maximize the study of the high–z population).

The scope of this paper is to provide a tool to estimate the detection rate of GRBs and, in particular, of high–z bursts. High–z GRBs are of particular relevance for planning forthcoming dedicated missions to study the high–z Universe. We have shown here the flux and fluence rate distributions considering four possible energy bands where present and future GRB detectors can operate. The presented curves can be used to estimate approximately the detection rates expected for an instrument operating in a given energy range and with a given sensitivity threshold.

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APPENDIX

We show in Fig.10 the cumulative distributions of the peak flux in units of erg cm\(^{-2}\) s\(^{-1}\) and in Fig.11 of the fluence in units of ph cm\(^{-2}\). In the results presented in the paper we have assumed a density evolution of the GRB formation rate with a constant luminosity function, i.e. a broken power law (\(\S\)). If the evolution is instead assigned to the luminosity function, we adopt the model parameters of Salvaterra et al. (2012) where there is an evolution of the cut of the luminosity function \(L_{\text{cut}} \propto (1+z)^2\). This evolution increases the number of high luminosity GRBs at high redshifts. Fig.12 compares the cumulative peak flux distribution obtained with the assumption of a density evolution of GRBs (\S\) - solid lines) and with the assumption of a luminosity evolution (dashed lines in Fig.12).

The other main hypothesis of our paper is the existence of the \(E_{\text{peak}} - E_{\text{iso}}\) and \(E_{\text{peak}} - L_{\text{iso}}\) correlations. It has been discussed that these could boundaries in the corresponding planes and some instrumental/observational effects prevent the exploration of the part of the planes which would be uniformly filled with intermediate/low \(E_{\text{iso}}(L_{\text{iso}})\) bursts. We have tested this possibility with our code and show in Fig.13 our results. We have assumed the \(E_{\text{peak}} - E_{\text{iso}}\) and \(E_{\text{peak}} - L_{\text{iso}}\) correlations, as obtained from the current data, and assumed that they divide the plane into two regions: the right hand side of these correlation is free of bursts, since if any GRB would be in this semi-plane it should have been detected, while the left hand side of the correlation is filled (uniformly) with bursts which have their peak energy uncorrelated with the \(E_{\text{iso}}\) or \(L_{\text{iso}}\). The boundary of the uniformly filled semi-plane are defined assuming that bursts have \(E_{\text{peak}} \in (0.01; 10^4)\) keV. This different assumption produce a flux cumulative distribution (dashed line in Fig.13) which is only slightly different from that obtained assuming the correlations as they are observed with their actual scatter (solid lines in Fig.13).

Figure 10. Cumulative distributions of the peak flux (in units of erg cm\(^{-2}\) s\(^{-1}\)). Same lines and color coding of Fig.4.

Figure 11. Cumulative distributions of the fluence (in units of ph cm\(^{-2}\)). Same lines and color coding of Fig.8.

Figure 12. Cumulative distributions of the peak flux comparing the results obtained assuming the evolution of the GRB formation rate (solid lines \(-\S\)) and the evolution of the luminosity function (dashed lines). Same lines and color coding of Fig.4.

Figure 13. Cumulative distributions of the peak flux comparing the results obtained with the assumptions of \S\) (solid lines) and that the \(E_{\text{peak}} - E_{\text{iso}}\) and \(E_{\text{peak}} - L_{\text{iso}}\) correlations are boundaries in the corresponding planes (dashed lines). Same lines and color coding of Fig.4.