Title

Assessment of Cerebral Autoregulation in Stroke: A Systematic Review and Meta-Analysis of Studies at Rest

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Short title

Assessment of Cerebral Autoregulation in Stroke
Abstract

Dynamic cerebral autoregulation (dCA) has been shown to be impaired in cerebrovascular diseases, but there is a lack of consistency across different studies and the different metrics that have been proposed for assessment. We performed a systematic review and meta-analyses of studies involving assessment of dCA in ischemic and hemorrhagic stroke. 32 articles describing assessment of dCA with transfer function analysis (TFA) were included, with meta-analyses performed for derived parameters of gain, phase and autoregulation index (ARI).

A total of 1233 patients were pooled from 12 studies on acute ischemic stroke (AIS) and two studies on intracerebral hemorrhage (ICH). In comparison with controls, TFA phase of AIS was significantly reduced (9 studies), in both hemispheres (p<0.0001). TFA gain provided inconsistent results, with reduced values in relation to controls, for both hemispheres. The ARI (6 studies) was reduced compared to controls, in both hemispheres (p<0.005). In ICH, gain showed higher values compared to controls for the unaffected (p=0.01), but not for the affected hemisphere.

Meta-analyses in AIS have demonstrated that phase and the ARI index can show highly significant differences in comparison with healthy controls, whilst ICH have been limited by the scarcity of studies and the diversity of units adopted for gain.
**Key Words:** cerebral blood flow, dynamic cerebral autoregulation, ischemic stroke, intracranial hemorrhage, transfer function analysis

**Introduction**

Dynamic cerebral autoregulation (dCA) is an important physiological marker in acute neurovascular pathology, with both prognostic and therapeutic significance, and is impaired in up to one third of patients following acute stroke.\(^1\)\(^2\) Impaired dCA has been studied in many cases of moderate to severe ischemic and hemorrhagic stroke, demonstrating damaged cerebral arterioles and capillaries, with related endothelial dysfunction, receptor impairment, and smooth muscle deactivation.\(^3\)\(^4\) These structural and functional changes lead to impaired vasomotor regulation and may contribute to the risks of hyper- or hypoperfusion, leading to secondary injury and worse outcomes.\(^5\)

Different cerebral blood flow (CBF) measurement modalities have been used for dCA assessment such as near-infrared spectroscopy (NIRS) and transcranial Doppler ultrasound (TCD). Most studies of dCA in stroke used TCD to obtain estimates of CBF by measuring CBF velocity (CBFV) in the middle cerebral artery (MCA) or other intra-cranial vessels.\(^6\) Although the thigh cuff maneuver was the original method used to demonstrate the phenomenon of dCA,\(^7\) and several other protocols have since been
advocated, the most common approach in clinical studies has been based on transfer function analysis (TFA), in conjunction with spontaneous fluctuations in arterial blood pressure (BP) and CBFV. By using BP as the ‘input’ and CBFV as ‘output’, TFA yields estimates of the amplitude (‘gain’) and phase of the BP-CBFV relationship as a function of the frequency of oscillations. The gain reflects how much of the amplitude of BP oscillations are attenuated by a working dCA at each frequency, whilst the phase expresses the time delay of CBFV changes following the BP oscillations. The autoregulation index (ARI), initially introduced to quantify the CBFV response to a thigh cuff maneuver, can also be extracted by TFA from spontaneous fluctuations of BP and CBFV. TFA parameters, including the ARI, have been reported to be altered in stroke patients. A recent international consensus White Paper is likely to improve inter-centre consistency for estimates of gain and phase, but their reliability for detecting loss of dCA function in cerebrovascular disease is largely unknown. To address this gap in knowledge, we performed a systematic review of the literature, including meta-analyses of gain, phase and ARI in studies of both ischemic and hemorrhagic stroke. Although some recent reviews have made reference to the application of TFA in studies of stroke, to our knowledge, this study is the first to perform a systematic review of this topic, with meta-analyses of gain, phase and ARI. The aims of this review were to assess the quality and quantity of evidence for TFA
parameters from dCA studies in acute stroke, to assess the heterogeneity of available evidence, and to identify knowledge gaps for future research.

**Materials and Methods**

Medline (1946-present), Embase (1947-present), Web of Science (1970-present), Psychinfo (1984-present), CIHNAL (1976-present) and The Cochrane Library (1993-present) were searched using the strategy provided in Supplemental Material. The search was limited to human studies in English, after 1990, as TFA application to dCA was first proposed by Giller et al\(^{17}\) in this year. The initial database search was conducted in August 2018, and was updated in May 2019 prior to submission. In addition, reference lists from all included studies and related papers were screened in PubMed for additional relevant articles. The protocol was registered on PROSPERO for this review prior to initiation (CRD42018109435). The PRISMA flow diagram of articles in this review is provided in Fig. 1. Studies on neurological diseases, subjected to qualitative analysis (Fig. 1) were further limited to ischemic and hemorrhagic stroke for the purposes of meta-analysis and detailed systematic review. Studies were screened initially by title and abstract by one reviewer (KI), and 10% were checked by a second reviewer (LCB). Included studies were independently evaluated as full papers by two reviewers against the inclusion and exclusion criteria (KI, LCB). Quality assessment was undertaken using pre-defined criteria which have been published previously,\(^{16, 18}\)
and summary charts and tables for risk of bias were constructed using the quality assessment criteria in RevMan© version 5.3 for Windows (Supplementary Figures 1 and 2). All data were extracted into Microsoft Excel for Windows by one reviewer (KI), and were then quality evaluated by a second reviewer (LCB).

**Inclusion criteria**

1) Adults aged >18 years; 2) Diagnosis of cerebrovascular diseases as defined by standard criteria; 3) Transfer function analysis metrics (gain, phase, coherence, or ARI) present; 4) dCA assessment in clinical population.

**Exclusion criteria**

1) Adults aged under 18 years; 2) Healthy population; 3) No TFA measures as listed above; 4) Non-cerebral autoregulation assessment.
RevMan5 software© for Windows, using the inverse variance method with random effects model was used to perform meta-analyses for possible heterogeneity of studies, based on the DerSimonian and Laird approach.\textsuperscript{19, 20} These methods can be found in detail in the Cochrane Handbook for Systematic Reviews of Interventions\textsuperscript{19} and statistical algorithms for Review Manager 5.\textsuperscript{21} In brief, this approach assumes that the included studies are estimating different but related effects.\textsuperscript{19} Using the inverse variance method, an estimate of the between-study variance is calculated (\textit{Tau}^2), where \textit{Tau} represents the estimated standard deviation of the underlying effects from the studies included in the analysis.\textsuperscript{19} The between study variance is determined by comparing the fixed effect, inverse variance result for each individual study.\textsuperscript{21} The 95\% confidence intervals for the range of these underlying effects are calculated as 2 x \textit{tau} above and below the pooled estimate.\textsuperscript{19} The inverse variance method adjusts the contribution of each individual study to the pooled estimate by applying weighting to each study dependent on the variation and heterogeneity (the reciprocal of the study variance or square of the standard error).\textsuperscript{19, 21} The units of phase were expressed in degrees, converting from radians whenever necessary, and the mean differences (MD) between patients and controls were calculated. Since gain had heterogeneous units that could not be converted to a common unit (absolute or normalised unit) as recommended in the White paper,\textsuperscript{14} the standardised mean differences (SMD) were calculated. The heterogeneity of studies were described as \textit{I}^2 index which indicates the percentage of
variation. Heterogeneity was low when $I^2 < 25\%$, moderate for $I^2 = 26$ to 74\% and $I^2 \geq 75\%$ was considered high and significant if $P < 0.01$. Pre-defined criteria for meta-analysis were: at least two studies with the same clinical population, same TFA parameter (phase, gain or ARI), and with sufficient homogeneity between the two or more studies (heterogeneity $I^2$ score < 75\%). Meta-analysis was not performed if there were less than two measurements in the same vessel for the same parameter, standard deviation was not provided, or data were not provided for controls and patients. Where studies measured both MCAs, affected and unaffected were separately categorised to prevent double-counting participants. In studies where only one control group was present, the same controls were used for each of the patient groups within a single study. Sensitivity analyses were carried out where the control participants were double counted.
Results

Summary of included studies

33 studies were included comprising 18 on AIS (large artery stroke, one study that also included transient ischemic attack (TIA)), 12, 13, 26-41 six on ICH, 42-47 three on small artery stroke, including lacunar infarction, 48-50 and six on AIS both large and small artery stroke 2, 23-25, 51, 52.

Study quality

The quality of included studies ranged from 10 to 15 (median 14, IQR 13-15) (Supplemental Table I).

Participant characteristics

From 33 studies of cerebrovascular disease (AIS including small and large artery and ICH), there was a total of 1233 participants (1010 subjects for AIS and 223 cases of ICH). In the AIS group, both large (n = 735 cases) and small artery (n = 275) strokes were included. The majority of studies reported the National Institutes of Health Stroke Scale (NIHSS) for categorising stroke severity, mean ranging from 0.7 to 22, 2, 12, 13, 23, 24, 26, 27, 29, 34-40, 49, 51, 52 three studies used degree of intracranial artery stenosis 28, 32, 41 and there were four studies where severity remained unclear. 25, 30, 33, 50 Eleven studies presented the modified Rankin Scale (mRS). 13, 24, 27, 29, 32, 35-38, 43, 46 Moreover, the
majority of participants were recruited within 6 to 72 hours from stroke onset,\textsuperscript{2, 12, 13, 24-27, 29, 34-40, 42, 43, 45-47, 49, 51} five studies assessed dCA at 48 hours (n = 8),\textsuperscript{2, 25, 34-36, 39, 47, 49} twenty-four hours were studied in four studies,\textsuperscript{37, 42, 43, 46} three studies examined dCA between 30 to 37 hours,\textsuperscript{12, 13, 38} dCA was assessed at 6 hours (n = 2),\textsuperscript{26, 27} one study assessed between onset to 16 days,\textsuperscript{52} other three studies recruited participants after first week of stroke onset\textsuperscript{32, 33, 48} and one study examined recovery at 6 months.\textsuperscript{49} The location of the lesion was identified in the MCA (n = 13),\textsuperscript{23, 26-28, 33-37, 40, 41, 49, 51} posterior cerebral artery (n = 3),\textsuperscript{31, 32, 49} and anterior cerebral artery territories (n = 3),\textsuperscript{2, 25, 52} though eight studies did not specify the precise localization of the lesion.\textsuperscript{12, 13, 24, 29, 38, 39, 48, 50} Five studies of ICH recruited participants for dCA testing within 48 hours of onset,\textsuperscript{42, 43, 45-47} with the exception of one study which assessed at 4-6 days after onset.\textsuperscript{44}
Transfer function analysis parameters

The results of TFA are usually interpreted with metrics of gain and phase or ARI. The majority of studies (n = 20) showed the results of gain and phase, six studies also included the ARI, five studies showed only phase and one article presented only gain for interpreting dCA45 (elementary Table 2). TFA results were presented in different units; the majority of studies (n = 9) reporting unit of gain as cm/s/mmHg, six studies as %/%, four studies as %/mmHg with dB and amplitude used for one study each. Two units were used for phase with twenty four studies presenting degrees and four studies using radians.

Phase by affected and unaffected hemispheres

Data were pooled from nine studies by using the mean difference (MD). Phase was significantly lower in AIS compared to controls, for both the affected (MD: \(-20.16, \text{CI: -28.80 to -11.52, } P < 0.00001\)) and unaffected hemispheres (Figure 2B; MD: \(-14.61, \text{CI: -24.21 to -5.01, } P = 0.003\)). Moreover, with large vessel occlusion (n = 8), phase was significantly lower in the affected AIS hemisphere, compared to controls (Figure 3A; MD: \(-15.73, \text{CI: -25.10 to -6.36, } P = 0.001\)), but not in the unaffected hemisphere (Figure 3B). In a pooled analysis of small artery stroke in four studies, phase was significantly lower in AIS, compared to controls in both the affected (Figure
4A; MD: -26.63, CI: -33.96 to -19.30, \( P < 0.00001 \)) and unaffected hemispheres (Figure 4B; MD: -27.11, CI: -32.17 to -22.04, \( P < 0.00001 \)).

Gain by affected and unaffected hemispheres

Six studies were included for meta-analysis. Gain was significantly lower in AIS compared to controls for both the affected (Figure 5A; SMD: -0.75, CI: -1.49 to -0.02, \( P = 0.04 \)) and unaffected hemispheres (Figure 5B; SMD: -0.85, CI: -1.61 to -0.09, \( P = 0.03 \)). On subgroup analysis, gain was significantly lower in patients with small vessel disease compared to controls for both the affected (\( n = 3 \)) (Figure 6A; SMD: -0.33, CI: -0.063 to 0.03, \( P = 0.03 \)) and unaffected hemispheres (Figure 6B; SMD: -0.44, CI: -0.75 to -0.14, \( P = 0.004 \)). However, there were no significant differences in five studies of large artery stroke in both hemispheres (elementary Figure 3).

ARI by affected and unaffected hemispheres

ARI of mild AIS decreased in the affected hemisphere at 36 hours post-event and was worse in both hemispheres at 96 hours after onset,\(^{12}\) remaining lower at two weeks after onset\(^ {13}\) and apparently diminished in a group of coexisting large and small artery stroke compared with individual large or small artery stroke.\(^ {52}\) However, ARI did not show a significant difference between affected and unaffected hemispheres in patients with TIA\(^ {12}\) and AIS.\(^ {25, \ 38}\) When pooling four studies, the affected side showed highly significantly reduced ARI in AIS compared to controls (Figure 7A; MD: -0.79, CI: -
1.28 to -0.30, \( P = 0.002 \), and also on unaffected side (Figure 7B; MD: -0.52, CI: -0.88 to -0.16, \( P = 0.005 \)).

**TFA examined over serial measurements in ischemic stroke patients**

Six studies performed serial assessments of dCA in AIS. Four studies measured dCA at similar time points: 0-2 days and 3-7 days, of which three reported only phase\(^{24, 34, 36}\) and one reported phase and gain.\(^{35}\) However, one study measured dCA at 1 week, 6 weeks and 3 months follow up,\(^{33}\) and another did not present the results of phase\(^{37}\) and these were therefore excluded from meta-analyses. Pooled analyses of the affected hemisphere demonstrated phase did not significantly differ in all participants between 0-2 days and 3-7 days after stroke onset (Supplementary Figure 4A; MD: 3.61, CI: -0.38 to 7.59, \( P = 0.08 \)). On the unaffected side, phase showed no significant differences between serial measurements (Supplementary Figure 4B). However, a tendency towards higher phase on 0-2 days in both hemispheres was observed in large artery stroke and one study showed bilaterally lower gain at 0-2 days.\(^{35}\) Nevertheless, two studies on the affected and unaffected hemispheres found a highly rebounding phase,\(^{34}\) and Kwan et al. also reported that there was a trend of increasing phase in both hemispheres when measurements were taken after 7 days from onset.\(^{33}\)

**Dynamic CA in ICH**
Two studies were selected for meta-analysis, with one study reporting both phase and gain\textsuperscript{43} and the other only gain.\textsuperscript{45} Excluded studies addressed vasospasm and delayed cerebral ischemia with ICH,\textsuperscript{47} did not report SD,\textsuperscript{46} used the same data from another study,\textsuperscript{43, 44} or did not identify the side of the lesion.\textsuperscript{42} Therefore, two articles were included for gain but none for phase. In the affected hemisphere, gain did not show a significant difference between ICH and controls (Figure 8A, SMD: 0.68, CI: -0.05 to 1.40, $P = 0.07$), but tended to favour ICH patients. However, in the unaffected hemisphere, gain was significantly higher in patients when compared to controls (Figure 8B, SMD: 0.98, CI: 0.21 to 1.74, $P = 0.01$). Although, phase could not be meta-analysed, individual studies showed a significantly lower phase in ICH when compared to controls.\textsuperscript{42-44}

**Discussion**

The majority of existing studies on dCA disturbances during the acute stage of stroke report that worse dCA within a week after onset may be predictive of poor clinical outcomes.\textsuperscript{27, 29, 32, 36, 37, 43, 46} Although there are currently standardized recommendations for measuring TFA in the context of dCA research,\textsuperscript{14} this tends to apply only to healthy studies. TFA is a non-invasive technique that can be applied safely and easily to a wide
range of clinical conditions, but there is currently no systematic review with associated meta-analysis of TFA for assessment of dCA in neurological applications.

Main findings

To our knowledge this is the first systematic review and meta-analysis to demonstrate that TFA is an effective tool for quantitative and qualitative assessment of dCA in acute stroke. TFA parameters consistently detected changes in dCA in AIS. TFA parameters (phase and ARI) demonstrated significantly impaired autoregulation in AIS patients compared to controls in meta-analysis, especially analyses in all stroke types, large and small artery stroke, and in both affected and unaffected hemispheres. However, dCA remained largely intact in the unaffected hemisphere in large territory stroke. There was significant heterogeneity on meta-analysis of the included studies, with variation in study setting, stroke population, and parameters measured. Despite this, results remained consistent between studies, and were statistically significant on pooled analyses, concluding that impaired autoregulation is present in AIS across stroke sub-types.

Phase

Phase was the parameter used by the majority of studies in this review to assess autoregulation, and also showed the most significant disturbance in AIS compared to controls. In terms of stroke sub-types, phase was significantly reduced in the affected
hemisphere in large artery stroke, and bilaterally in small vessel stroke. Studies that conducted serial measurements demonstrated a tendency towards lower phase at 3-7 days compared to 0-2 post-event. Given that phase was the most consistently reported parameter, showing the greatest change, and with the ability to discriminate between stroke sub-types, this would suggest phase is advantageous over other commonly reported TFA parameters for the assessment of dCA in AIS.

**ARI**

ARI was significantly reduced in both hemispheres in all studies of AIS compared to controls. Although individual studies did not demonstrate significant changes in ARI, this was highly significant on pooled analyses, suggesting thus far that studies have been under-powered to detect these changes. In comparison to phase and gain, the ARI was also disadvantaged by studies dominated by strokes of lesser severity. An important consideration is the fact that calculation of the ARI includes all the information from phase and gain, and therefore has the potential to perform equally or better than these parameters. Moreover, the ARI can be seen as an inter-method ‘currency’ that can be adopted with other protocols, such as the thigh cuff maneuver, that do not utilise TFA.

**Gain**
Only two studies demonstrated a higher gain on the affected\textsuperscript{23, 40} and unaffected hemispheres\textsuperscript{23} in AIS patients. However, on pooled analyses, gain was significantly lower (signalling better autoregulation) in AIS compared to control. This is in contrast to the findings on pooled analyses of phase and ARI of poorer autoregulation in AIS compared to control. These results are unexpected, as the gain would be anticipated to be high in AIS pathology, particularly in the affected hemisphere, as a result of reduced ability of the brain to dampen the effects of BP on CBFV due to impaired vasomotor activity.\textsuperscript{53} There are a number of potential explanations for this unexpected result. Firstly, there was significant heterogeneity in the pooled analysis as a result of frequency range for dCA assessment (Supplemental Table II). Secondly, the results reported here are SMD due to variation in the units reported between studies. Thirdly, the reliability of gain as a marker of impaired autoregulation may not be as robust as that of phase and ARI.\textsuperscript{6} This is as a result of methodological variations in the calculation and reporting of gain as a parameter, leading to significant concerns in its interpretability and validity as a measure of dCA.\textsuperscript{6} Finally, nonstationary dCA behaviour might be more strongly manifested in longitudinal changes in gain, when compared to other parameters such as phase or ARI.\textsuperscript{54}

\textit{ICH}

The results of ICH studies showed a lower phase in both hemispheres. Phase was also significantly lower during the early stage (1-6 days), and had a prolonged decreasing
phase with a further deterioration 7-13 days after ICH onset when compared with healthy controls.\textsuperscript{42-44} Autoregulatory capability appears to rebound by 30 days but does not fully recover.\textsuperscript{43} Perihematomal edema and hematoma size, as well as impaired Glasgow Coma Scale, may contribute to dCA impairment between 10 to 20 days after ictus.\textsuperscript{16, 55} Moreover, meta-analysis in few ICH studies showed higher gain in both hemispheres of ICH patients,\textsuperscript{43, 45} which reflects the poor dampening mechanism of regulators, though further studies are required for confirmation. Nonetheless, it appears that using TFA for assessment of dCA in clinical applications is valuable prior to management of blood pressure to prevent hypoperfusion leading to increased ischemic penumbra and hyperperfusion inducing cerebral edema.

\textit{Limitations of the study}

The major limitations of this review are: small sample sizes, a wide range of time points for TFA assessment of dCA after stroke onset, methodology and statistical analysis changing over time across studies, lack of detail regarding the location of the brain lesion in some studies, significant heterogeneity of pooled analyses and units of TFA measurement, inclusion of papers that did not follow the Cerebral Autoregulation Research Network (CARNet)’s White Paper recommendations,\textsuperscript{14} and lack of consideration of other modalities, such as NIRS, that could have greater sensitivity to detect affected tissue perfusion in certain brain regions. Although this review has
demonstrated clear and consistent abnormalities in dCA on pooled analyses, gain did
not follow the expected pattern of results, and further work is required to investigate the
reliability and validity of this parameter in comparison to that of phase and ARI in acute
stroke. Importantly, not all studies clearly followed the recommended methodology for
gain, limiting the interpretation of the results reported here. Despite clear
recommendations on the conduct and reporting of studies of TFA, few of those included
in this review were in line with these guidelines.¹⁴ Future studies of TFA in clinical
applications should adhere to this guidance to improve the quality of conduct and
reporting of studies, and facilitate better quality meta-analyses with lower heterogeneity.

Further work

Further prospective work on standardised TFA settings is necessary to reduce the
heterogeneity of outcomes. The diversity of timings for follow up assessments of dCA
should also be addressed. Dedicated studies with more frequent assessments of dCA,
ranging from the ultra-acute (hours) to the medium-term post stroke (weeks), would
improve our knowledge of the longitudinal course of dCA. Of considerable relevance,
thresholds for impairment of dCA in both AIS and ICH need to be established to allow
better patient stratification for patient prognostication and management and more robust
assessments of the role of dCA in patient outcomes.
Robust techniques and metrics are needed to move assessment of dCA from the research arena into routine patient care. In AIS, meta-analyses of TFA parameters, obtained from spontaneous fluctuations of BP at rest, have demonstrated that phase and the ARI index can show highly significant differences in comparison with healthy controls, whilst less clear-cut results were obtained for gain. Meta-analyses of TFA applications to ICH have been limited by the scarcity of studies and the diversity of units of measurement adopted for gain. Evaluation of dCA in the acute phase of stroke and other cerebrovascular diseases is essential for informed clinical management. This review has demonstrated that TFA has considerable potential as a diagnostic tool, although further work is needed to assess its prognostic value. Further work is also needed to establish the ability of TFA parameters to distinguish between different types, locations and severity of stroke, and to establish ranges of normality that take into account different phenotypes.

**Appendix** – Equations for calculation of TFA gain, phase and ARI

Using beat-to-beat values of BP as input and corresponding values of CBFV as output, the fast Fourier transform is applied with Welch’s method to produce estimates of the auto- and cross-spectra of BP and CBFV, represented as $S_{xx}(f)$ (BP), $S_{yy}(f)$ (CBFV) and $S_{xy}(f)$, respectively. From these quantities, the complex transfer function, $H(f)$ is calculated as:
\[ H(f) = \frac{s_{xy}(f)}{s_{xx}(f)} \]  

which can be expressed as the amplitude (or ‘gain’) and phase frequency responses, given by:

\[ G(f) = [H_R(f)^2 + H_I(f)^2]^{1/2} \]  
\[ \phi(f) = \tan^{-1}\left[\frac{H_I(f)}{H_R(f)}\right] \]

where \( G(f) \) is the gain and \( \Phi(f) \) is the phase as a function of frequency and \( H_R(f) \) and \( H_I(f) \) are the real and imaginary parts of \( H(f) \), respectively.

Finally, the magnitude squared coherence function (MSC), which reflects the degree of linear association between input and output is given by:

\[ \text{MSC}(f) = \frac{|s_{xy}(f)|^2}{s_{xx}(f)s_{yy}(f)} \]

**ARI equations**

The autoregulation index (ARI) was introduced by Tiecks et al. (1995), to quantify the CBFV response to a rapid change in BP, induced by the sudden release of pressurised thigh cuffs. A second-order linear differential equation was proposed to predict the CBFV signal \( V(t) \) following a pressure change \( P(t) \). Initially, the pressure change is normalised as:

\[ dP(t) = \frac{P(t)}{1-CrCP} \]

Where \( CrCP \) represent the critical closing pressure. The velocity response can be estimated as:
\[ \dot{V}(t) = 1 + dP(t) - K \times x_2(t) \]  \hspace{1cm} (6)

where \( K \) is a parameter of gain and \( x_2(t) \) is a state variable obtained from the following state equation system representing a second-order linear differential equation:

\[ x_1(t) = x_1(t-1) + \frac{dP(t-1)-x_2(t-1)}{f \times T} \]  \hspace{1cm} (7)

\[ x_2(t) = x_2(t-1) - \frac{x_1(t-1)-2 \times D \times x_2(t-1)}{f \times T} \]  \hspace{1cm} (8)

where \( f \) is the sampling frequency, \( T \) represents a time constant, and \( D \) is the damping factor. The parameter values of gain (\( K \)), time constant (\( T \)) and damping factor (\( D \)) are combined in a table [REF Tiecks 1995], corresponding to 10 values of ARI, ranging from zero (absence of CA) to 9 (best observed CA). When \( P(t) \) is represented by a sudden change in BP, or a step function, equations [6]-[8] can then be used to generate 10 theoretical CBFV step responses, each corresponding to a value of ARI.

CBFV step responses can be obtained by the inverse FFT transform of equation [1], and then compared to each of the 10 template step responses proposed by Tiecks et al (1995), using the least square procedure, to derive a value of ARI associated with spontaneous fluctuations in BP and CBFV.
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None.

Author Contribution Statement

KI and LB performed literature search and extracted information. KI performed meta-analyses. VJS, RBP and TGR conceptualised and planned study. KI, LB and RBP drafted manuscript. All authors revised draft and accepted final version of the manuscript.

Disclosure/Conflict of Interest

None.

Supplementary Material

Supplementary material for this paper can be found at

http://jcbfm.sagepub.com/content/by-supplemental-data
References


Figure legends

Figure 1. PRISMA flow diagram.

Figure 2. A: Forest plot of phase for the affected side in nine studies of AIS. Heterogeneity is high and also significant ($I^2 = 94\%, P < 0.00001$). B: Phase for the unaffected side of nine studies. Heterogeneity is high and significant ($I^2 = 94\%, P <$
0.00001). In a sensitivity analysis, removing studies\textsuperscript{23, 24} which used the same control participants did not alter the results.

Figure 3. A: Forest plot of phase for a sub-group of eight studies on the affected side in large artery stroke. Heterogeneity is high and also significant ($I^2 = 91\%, \ P < 0.00001$).

B: Phase for a sub-group of eight studies of the unaffected side in large vessel disease. Heterogeneity is high and also significant ($I^2 = 93\%, \ P < 0.00001$).

Figure 4. A: Forest plot of phase for a sub-group of four studies on the affected side in small artery stroke. Heterogeneity is moderate and non-significant ($I^2 = 62\%, \ P = 0.05$).

B: Phase for a sub-group of four studies on the unaffected side in small vessel disease. Heterogeneity is low and non-significant ($I^2 = 25\%, \ P = 0.26$).

Figure 5. A: Forest plot of gain for the affected side in six studies of AIS. Heterogeneity is high and significant ($I^2 = 91\%, \ P < 0.00001$). B: Gain for the unaffected side of six studies of AIS. Heterogeneity is high and also significant ($I^2 = 91\%, \ P < 0.00001$).

Figure 6. A: Forest plot of gain for a sub-group of two studies on the affected side in small artery stroke. Heterogeneity is low and non-significant ($I^2 = 0\%, \ P = 0.50$). B: Gain for a sub-group of two studies on the unaffected side in small vessel disease. Heterogeneity is low and non-significant ($I^2 = 0\%, \ P = 0.61$).
Figure 7. A: Forest plot of ARI for the affected side in four studies of AIS. Heterogeneity was low and non-significant ($I^2 = 37\%, \ P = 0.16$). B: ARI for the unaffected side in four studies of AIS. Heterogeneity was low and non-significant ($I^2 = 0\%, \ P = 0.99$). In a sensitivity analysis, removing studies 12, 25 which used the same control participants did not significantly alter the results.

Figure 8. Forest plots of gain for the affected side in two studies of ICH. Heterogeneity was high but non-significant ($I^2 = 70\%, \ P = 0.07$). Gain for the unaffected side in two studies of ICH. Heterogeneity was high but also non-significant ($I^2 = 71\%, \ P = 0.06$).